

Model of Heat and Mass Transfer with Moving Boundary during Roasting of Meat in Convection-Oven

COMSOL Conference

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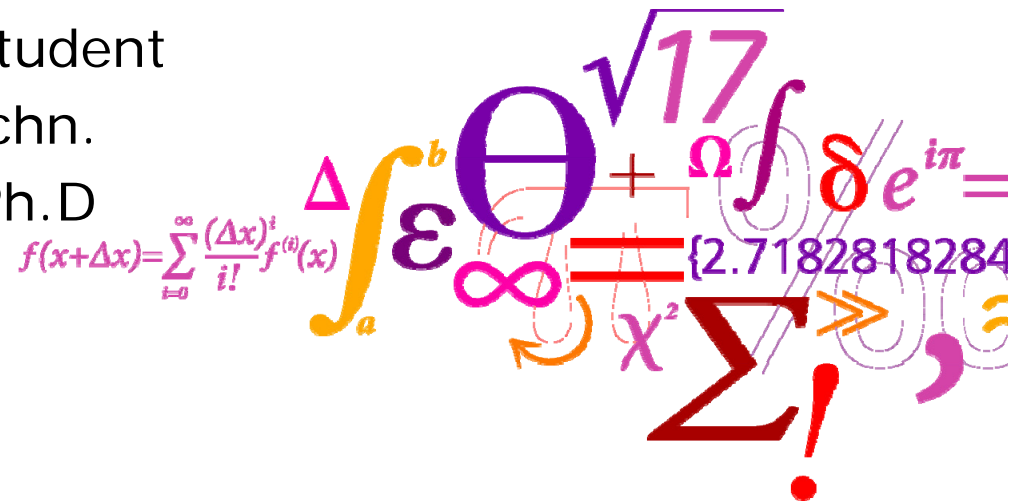
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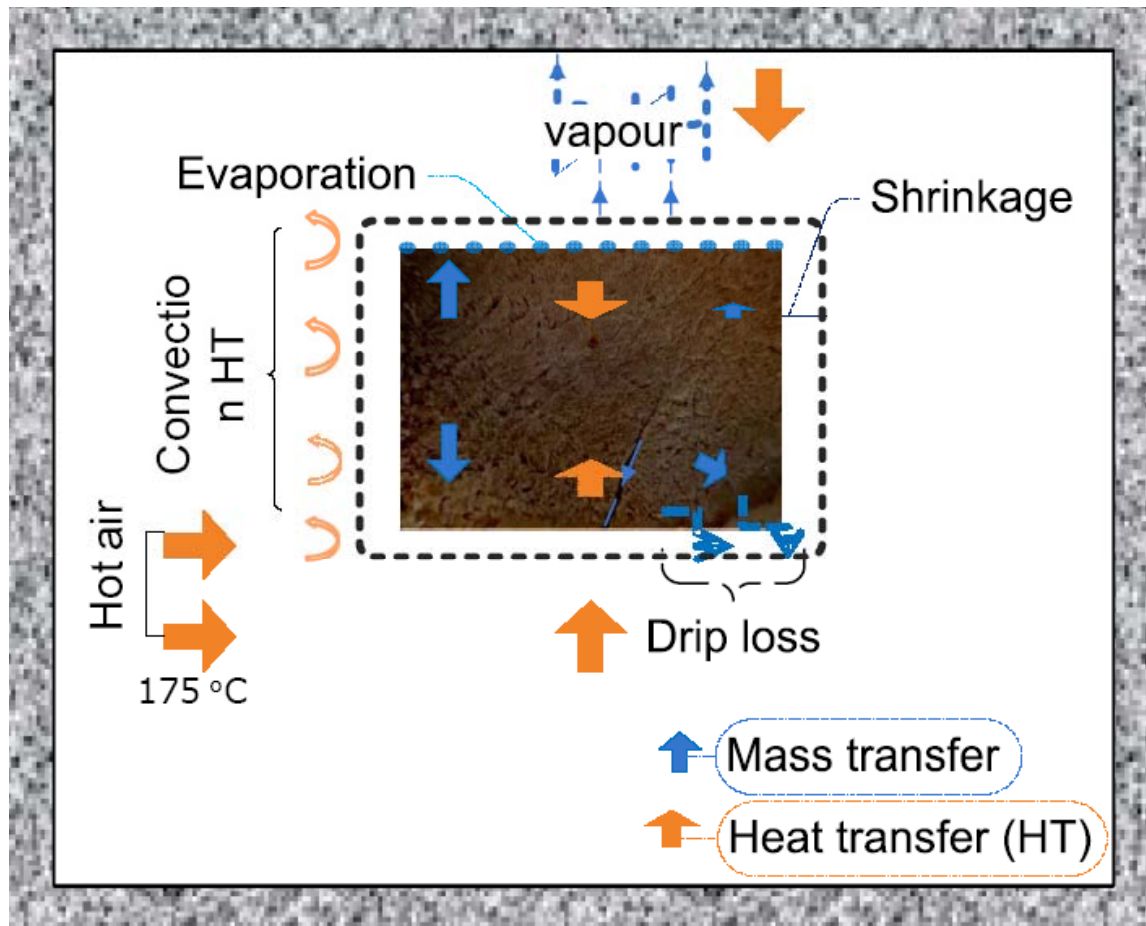
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Outline

- # Introduction
- # Theoretical background
- # Modelling
 - # Governing model equations
 - # Boundary and initial condition
 - # Model Solution
- # Results
- # Conclusion

Roasting process



Transport processes during oven-convection roasting

Model

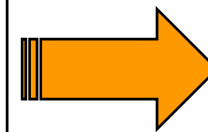
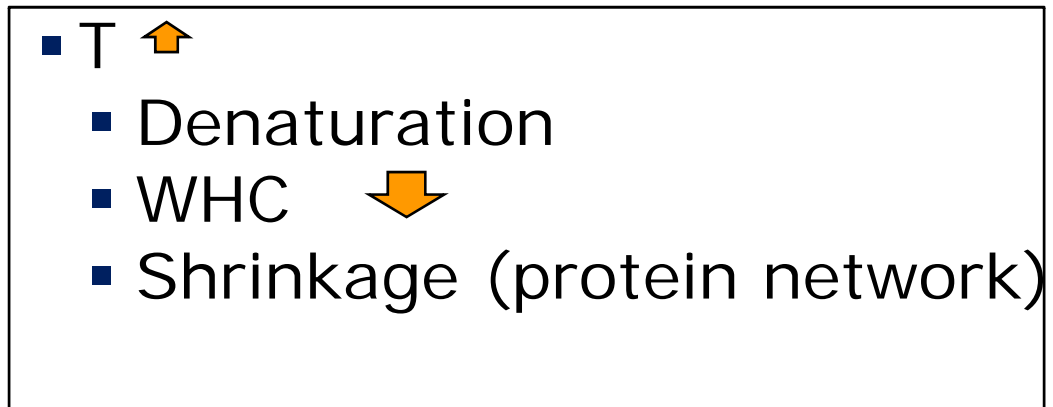
- Better quantitative knowledge
- Prediction of T, C
- Quality, safety
- Minimize loss
 - Mass and energy
- Upscale
- Process control

Water transport

✚ *Pure diffusion (often assumed)*

- But doesn't capture pressure

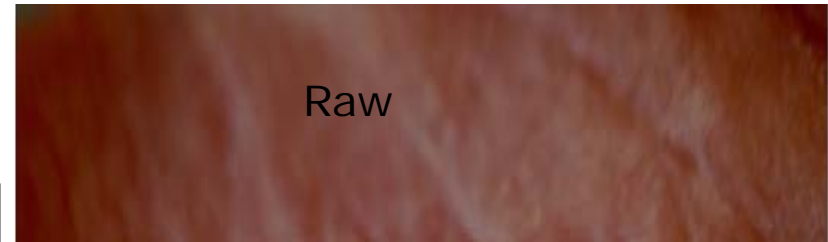
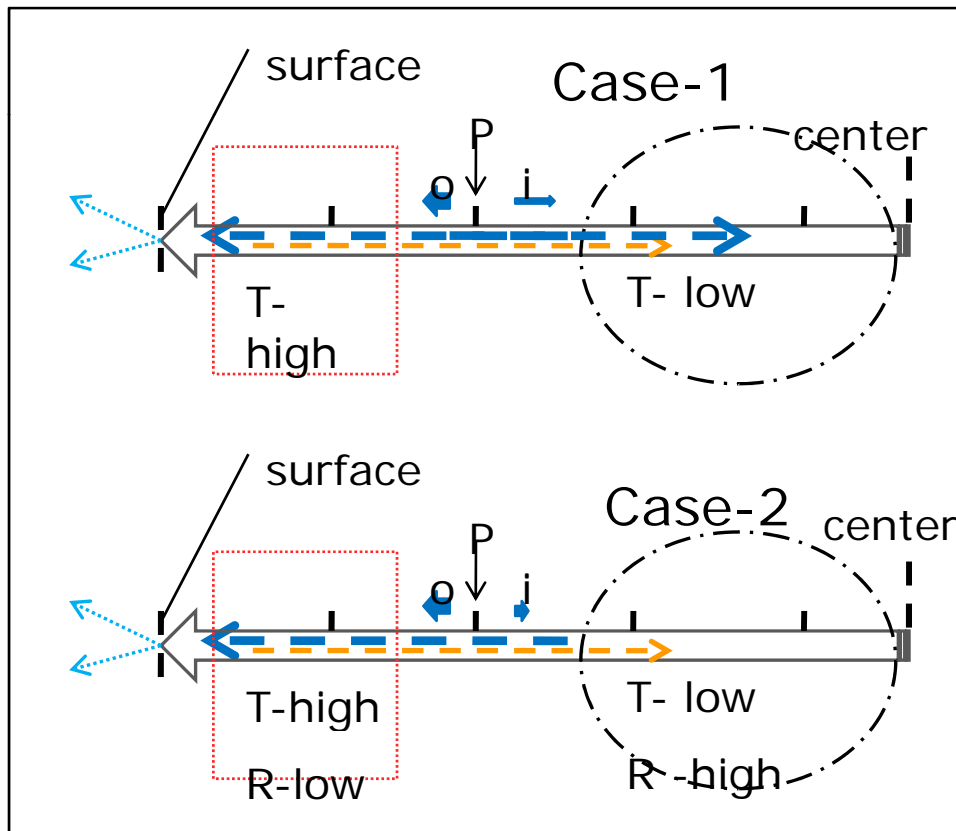
✚ *Convective*



Pressure
gradient
velocity

Change of microstructure

- Permeability (K)
- Elastic modulus (E)



Change of microstructure during roasting
(cross-sectional view)

Assumptions

- Fat transport is negligible (lean meat)
- Evaporation takes place at the surface
- No internal heat generation and no chemical reaction
- Dissolved matter lost with water is small
- Reduction of water holding capacity and shrinkage are considered.

Governing equation of heat and mass transfer

Heat transfer

$$\rho_m c_{pm} \frac{\partial T}{\partial t} + \nabla(-k_m \nabla T) + \rho_w c_{pw} u_w \nabla T = 0$$

$$\begin{aligned} \rho_m &= f(C) \\ D &= f(T) \\ c_{pm} &= f(C) \\ \mu_w &= f(T) \end{aligned}$$

Water transport

$$\frac{\partial C}{\partial t} + \nabla(Cu_w) = \nabla D \nabla C$$

Velocity of water

$$u_w = \frac{-K}{\mu_w} \nabla P$$

Darcy's law

$$P = E(C - C_{eq}(T))$$

$$u_w = \frac{-KE}{\mu_w} \nabla(C - C_{eq})$$

$$C_{eq}(T) = 0.75 - \frac{0.345}{(1 + 30 \exp(-0.25(T - T\sigma)))}$$

$$E(T) = E_o + \frac{E_{mx}}{(1 + \exp(-E_n(T - E_D)))}$$

Shrinkage /interface velocity

- ✚ Proportional to the volume of liquid water removed
- ✚ Formation of air filled pores

$$V = V_0 - \beta V_{w,l} \quad \beta = 1, \text{ no pore formation}$$

$$\beta = 0, \text{ no shrinkage}$$

$1 - \beta =$ fraction of $V_{w,l}$ replaced by air

$$V = V_0 \left(1 - \frac{\beta V_{w,l}}{V_0} \right)$$

$$= \pi R_0^2 \left(1 - \frac{\beta V_{w,l}}{V_0} \right)^{2/3} Z_0 \left(1 - \frac{\beta V_{w,l}}{V_0} \right)^{1/3} = \pi R^2 \cdot Z$$

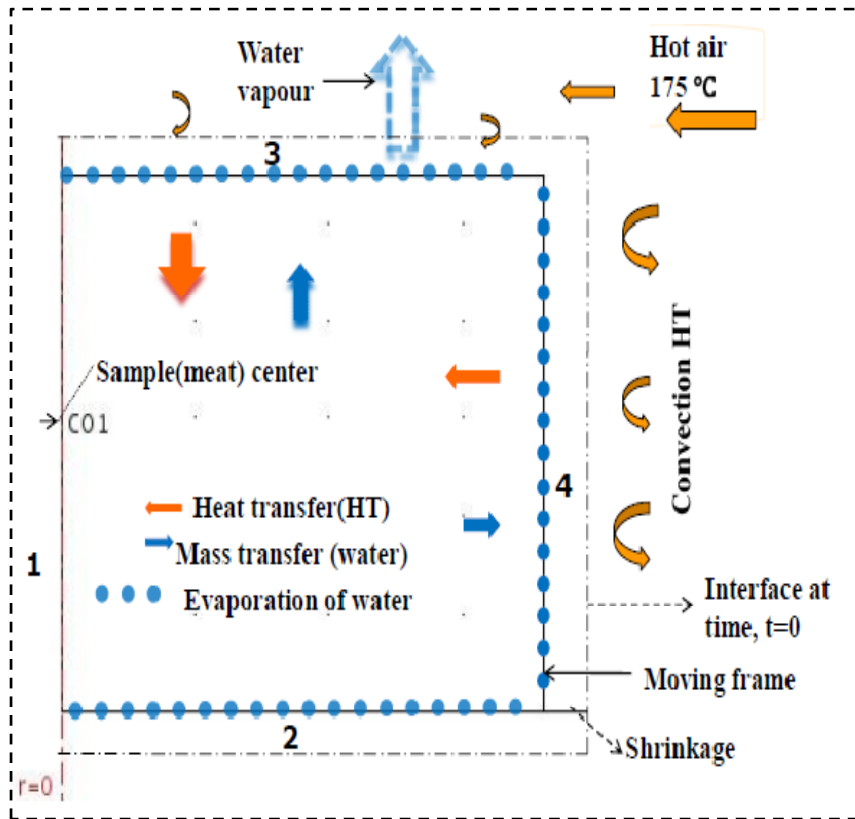
$$v_z = \frac{dZ}{dt} = -\frac{Z_0 \beta}{3V_0} \left(1 - \frac{\beta V_{w,l}}{V_0} \right)^{-2/3} \frac{d(V_{w,l})}{dt}$$

$$v_r = \frac{dR}{dt} = -\frac{R_0 \beta}{3V_0} \left(1 - \frac{\beta V_{w,l}}{V_0} \right)^{-2/3} \frac{d(V_{w,l})}{dt}$$

$$V_{w,l} = \frac{m_d(X_0 - X)}{\rho_w} = \frac{\rho_0 V_0 (1 - C_0)}{\rho_w} \left(\frac{C_0}{1 - C_0} - \frac{C_{av}}{1 - C_{av}} \right)$$

$$\frac{dV_{w,l}}{dt} = -\frac{\rho_0 V_0 (1 - C_0)}{\rho_w} \left(\frac{1}{1 - C_{av}} \right)^2 \frac{dC_{av}}{dt}$$

Boundary conditions and initial condition



BC 1:

Axial symmetry, $v_r=0$

BC (2, 3, and 4):

- HT- heat flux
- MT- mass flux
- ALE- velocity

IC:

$$T(r, z) = T_0 = \text{const} \quad \text{at } t = 0$$

$$C(r, z) = C_0 = \text{const} \quad \text{at } t = 0$$

Solution

- + COMSOL Multiphysics® version 3.5

- + 2D cylindrical

- Radius of 20 mm and length of 54 mm

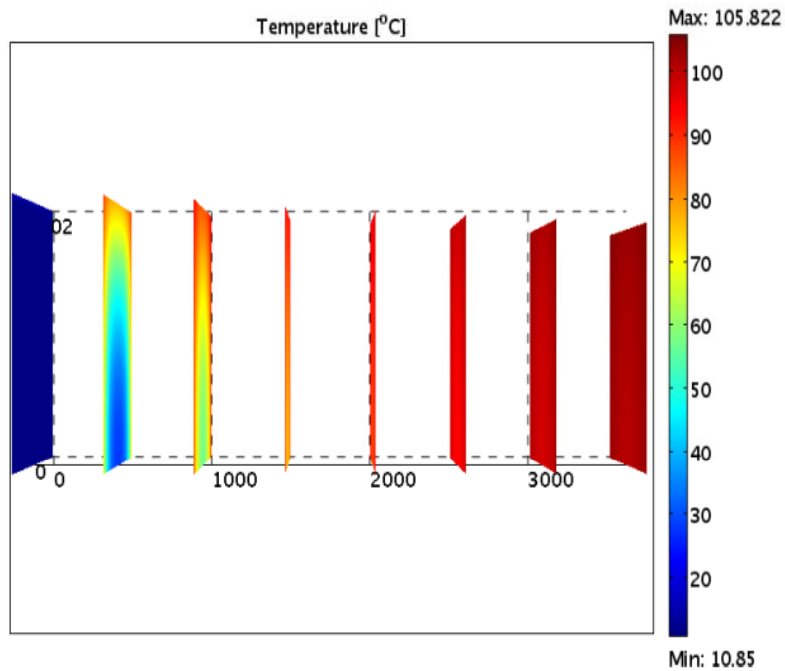
- + *Chemical Engineering module*

- Transient heat transfer

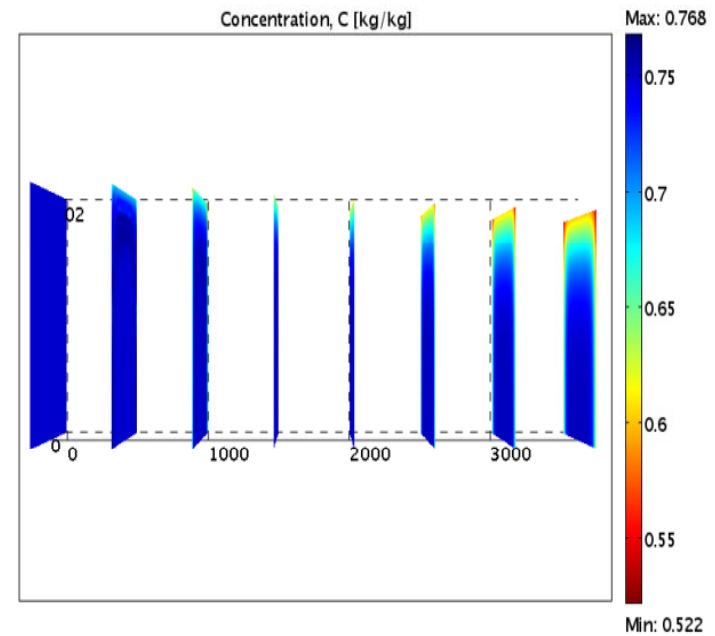
- Transient mass transfer

- + *Moving mesh module (ALE)*

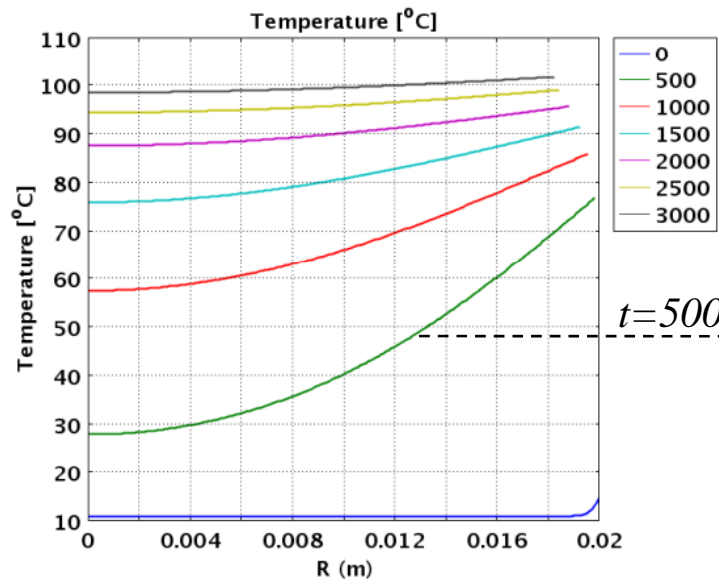
Results



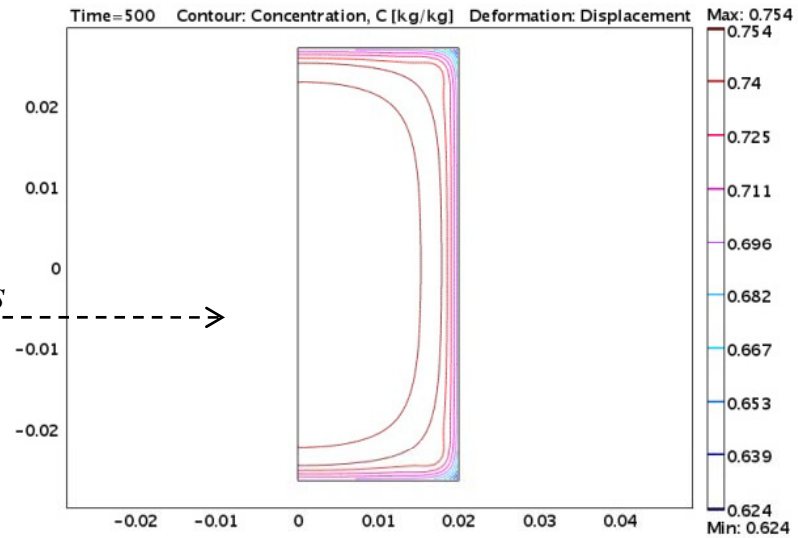
Temperature distribution



Water content distribution



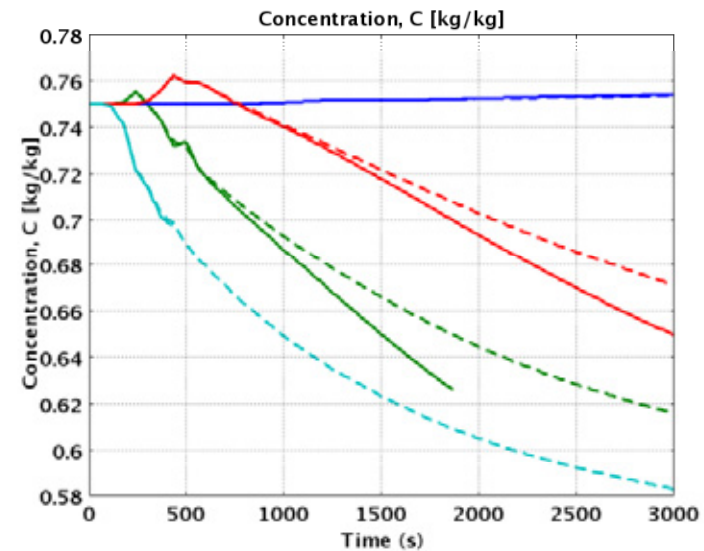
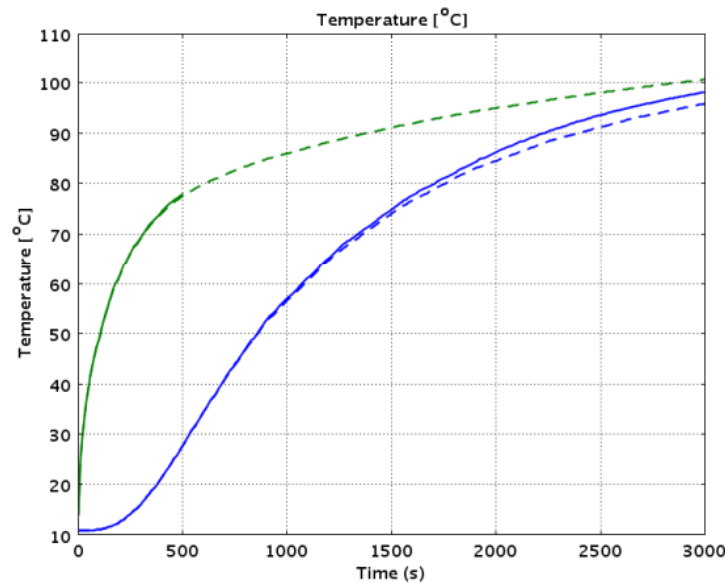
$t = 500s$



Temperature profile across cylindrical sample ($Z = 0$)

**Iso-concentration lines
C (kg/kg) at $t = 500 s$**

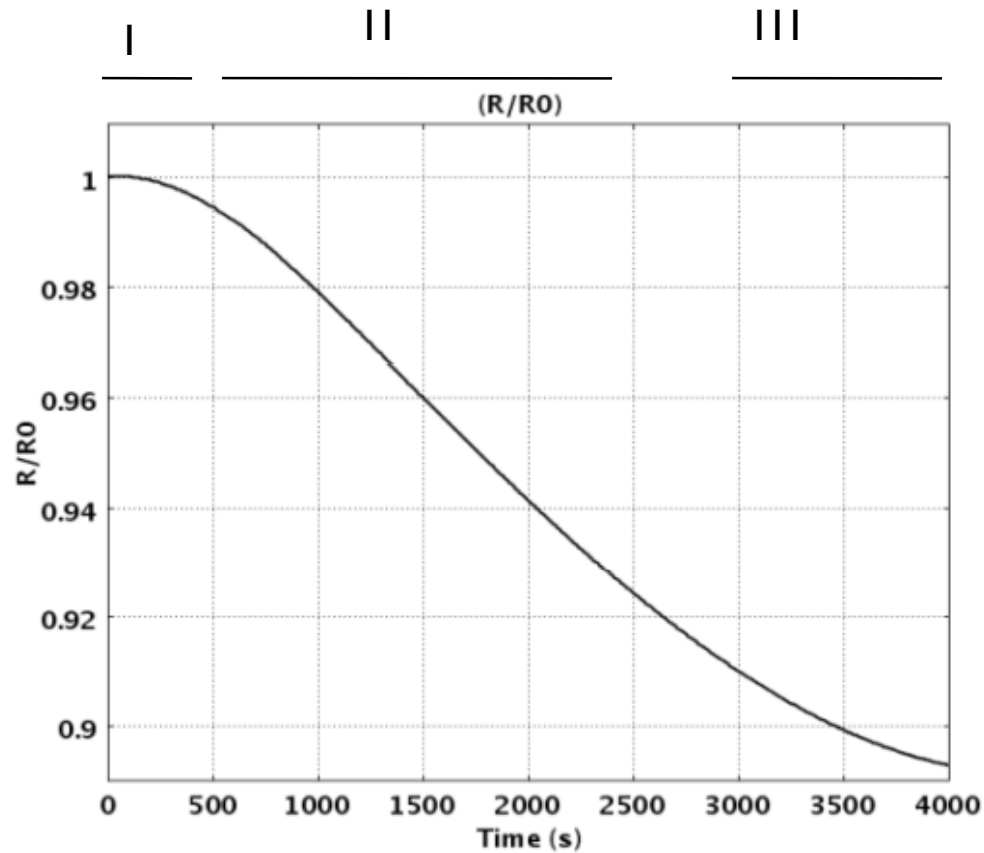
Model prediction with (-) MB vs. with FB (--)



Temperature profile
 blue-center(0, 0)
 green-surface ($r = 0.02, z = 0$)

Water content profile
 blue(0, 0), red (0.017, 0)
 green (0.019, 0), cyan (0.02, 0)

Radial shrinkage



Relative radius of cylinder as function of time (R/R0)

+ Conclusion

- A 2D model of HMT with MB is developed and models equations were solved using COMSOL for convection roasting process.
- Effect of WHC and shrinkage are incorporated.
- Better insight is obtained.

+ ACKNOWLEDGEMENT

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Thank you for your
attention!