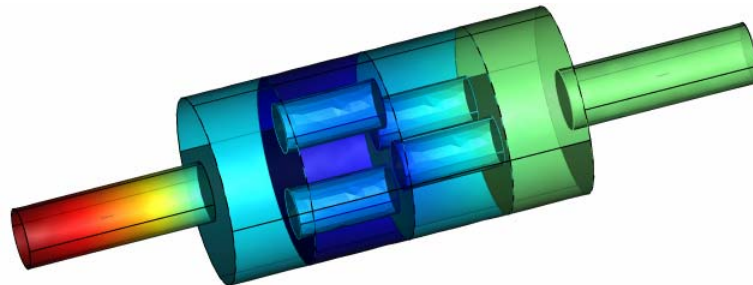


Analyzing Muffler Performance using the Transfer Matrix Method

By Kasper Steen Andersen,
Dinex Emission Technology A/S



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Content

- ▶ The Transfer Matrix Method
- ▶ The Numerical Models
- ▶ Results
- ▶ Conclusion



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Exhaust Systems in General

- ▶ Exhaust gas transportation
- ▶ Noise reduction
- ▶ NO_x, HC, PM reduction



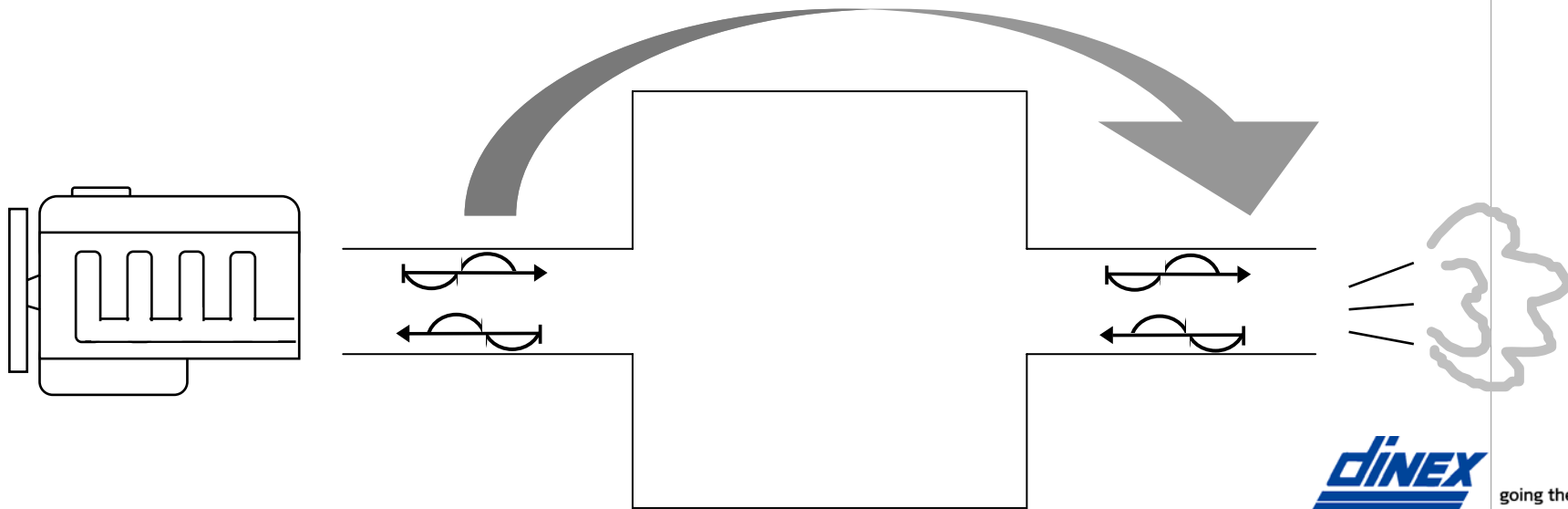
The Transfer Matrix Method



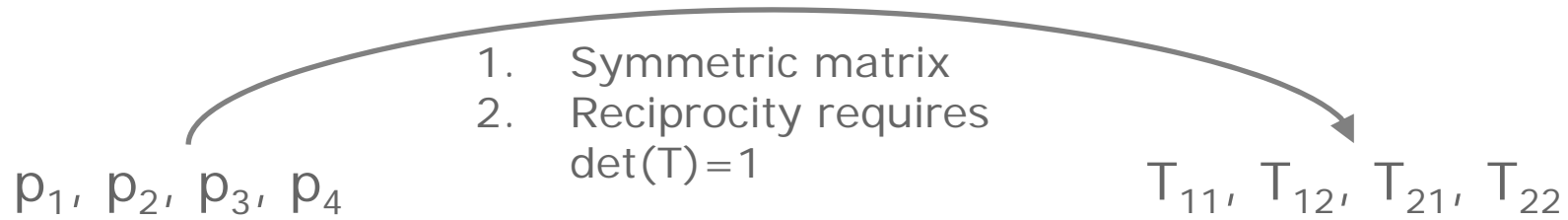
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The Transfer Matrix

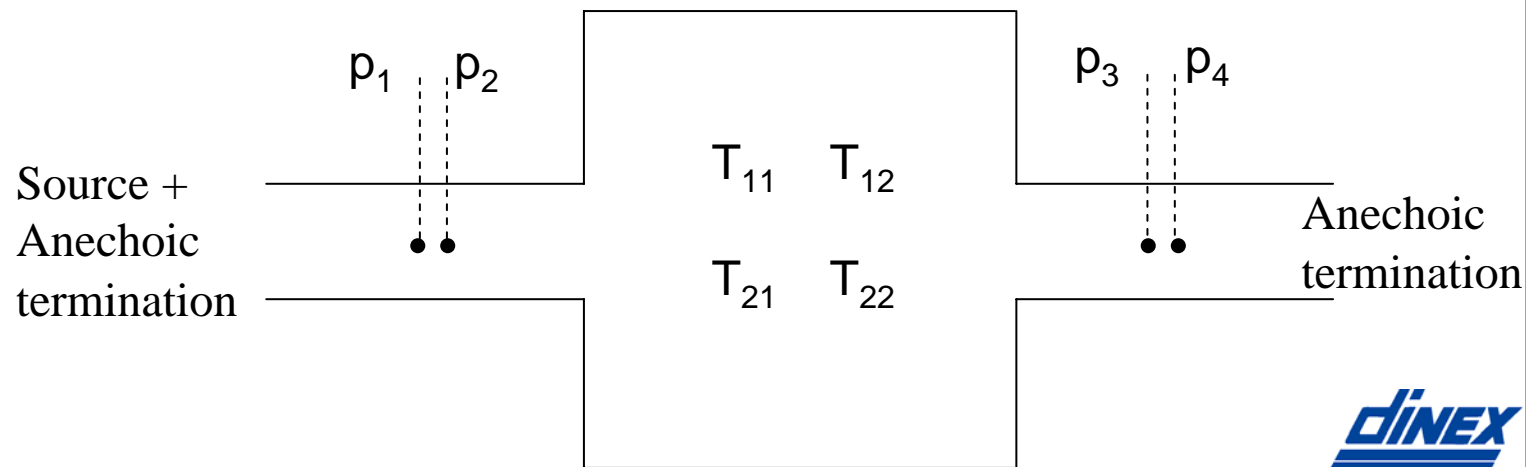
- ▶ The acoustical transfer properties of a system
- ▶ Plane wave decomposition in the connecting pipes



The Transfer Matrix Extraction



Advantage:
Solving the FEM problem only once



Evaluation Parameters

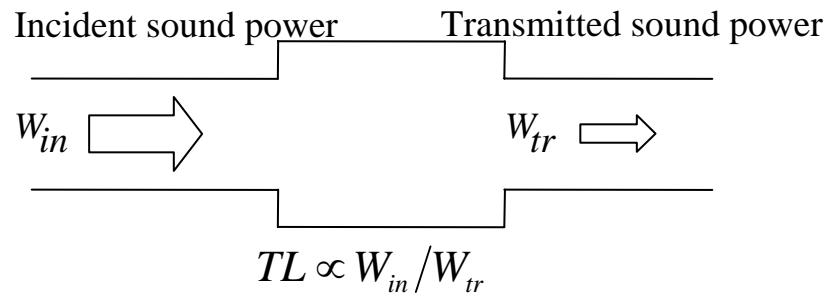
Transmission loss (source **in**dependent)

Insertion loss (source dependent)



Evaluation parameters

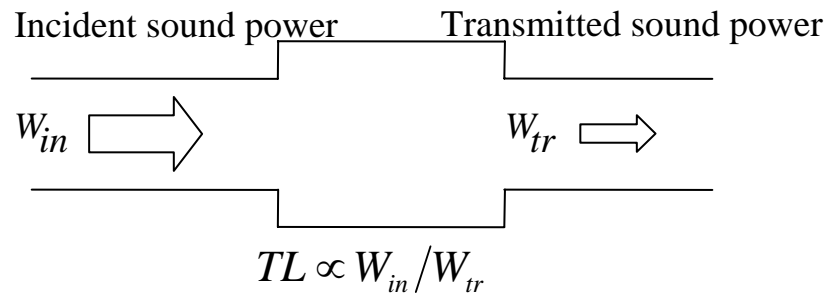
Transmission loss (source **in**dependent)



Insertion loss (source dependent)

Evaluation parameters

Transmission loss (source independent)

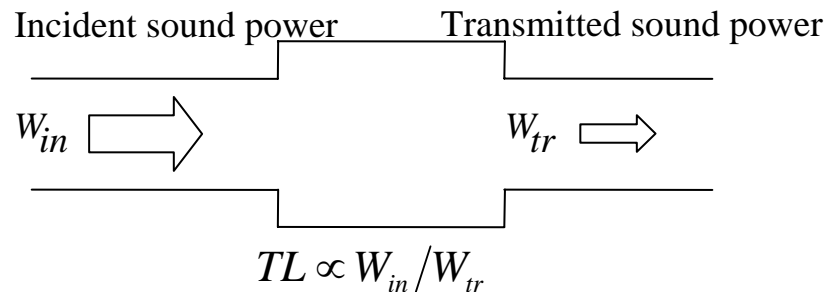


$$TL = 10 \log \left(\frac{1}{4} \left| T_{11} + T_{12} \frac{S}{\rho c} + T_{21} \frac{\rho c}{S} + T_{22} \right|^2 \right)$$

Insertion loss (source dependent)

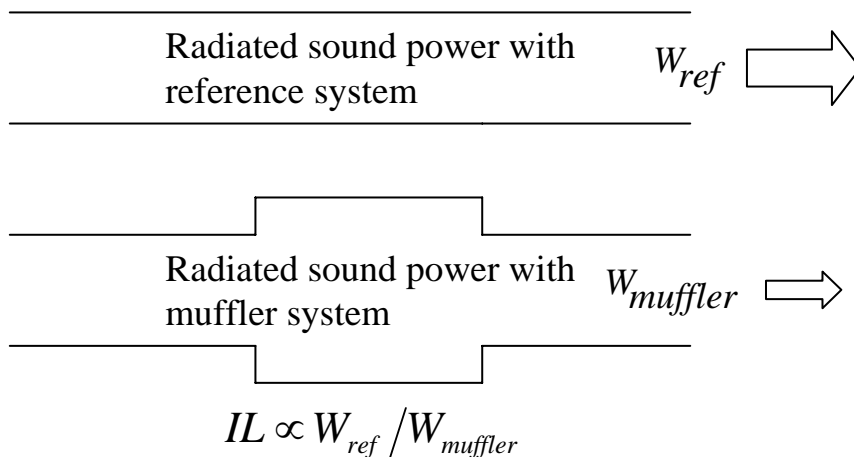
Evaluation parameters

Transmission loss (source independent)



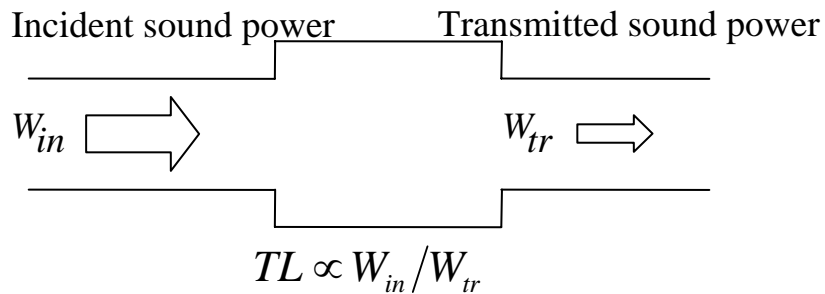
$$TL = 10 \log \left(\frac{1}{4} \left| T_{11} + T_{12} \frac{S}{\rho c} + T_{21} \frac{\rho c}{S} + T_{22} \right|^2 \right)$$

Insertion loss (source dependent)



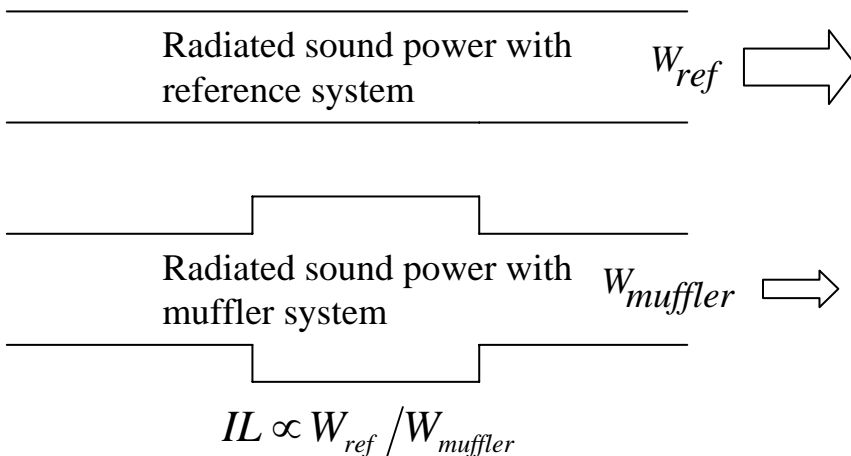
Evaluation parameters

Transmission loss (source independent)



$$TL = 10 \log \left(\frac{1}{4} \left| T_{11} + T_{12} \frac{S}{\rho c} + T_{21} \frac{\rho c}{S} + T_{22} \right|^2 \right)$$

Insertion loss (source dependent)



$$IL = 10 \log \left(\frac{|T_{11} Z_{a,r} + T_{12} + Z_{a,s} + (T_{21} Z_{a,r} + T_{22})|^2}{|T_{11}' Z_{a,r} + T_{12}' + Z_{a,s} + (T_{21}' Z_{a,r} + T_{22}')|^2} \right)$$

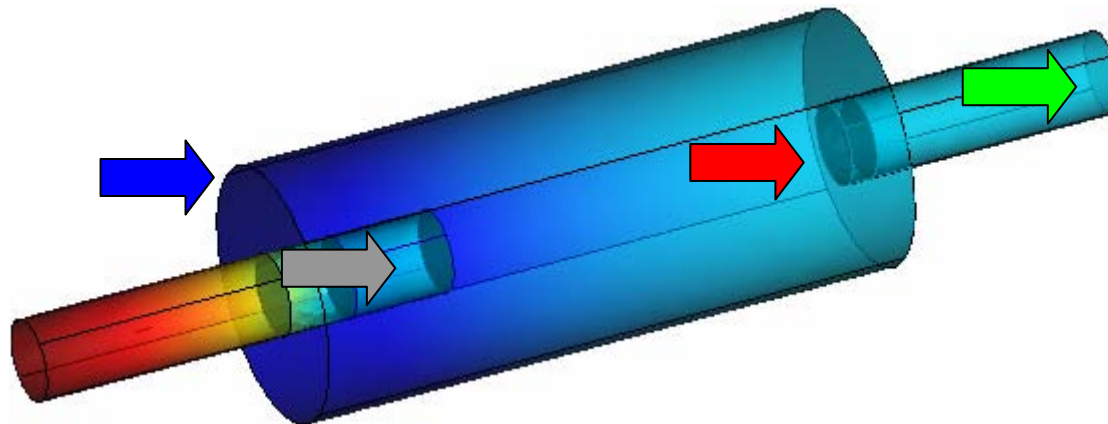
The Numerical Model



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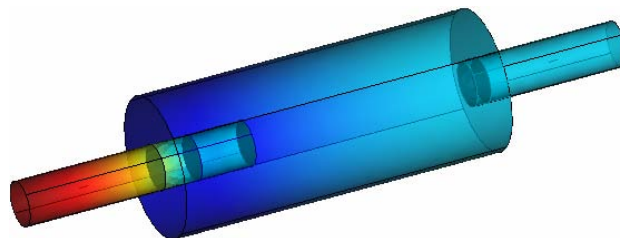
Boundary Conditions

- ▶ Solid walls (sheet metal)
- ▶ Coupling boundaries conditions (wave propagation from one medium to another)
- ▶ Radiation conditions (reflection free ends)
- ▶ Impedance conditions (perforated plates)



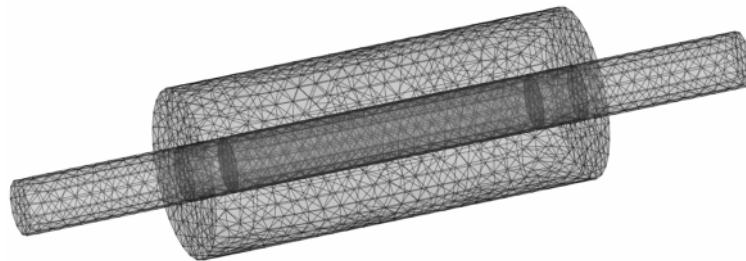
Subdomain Conditions

- ▶ Air
 - ▶ Defined by the speed of sound and the density
- ▶ Absorptive material
 - ▶ Defined by the apparent density and average fiber diameter
 - ▶ Based on theory by Delany and Bazley, Bies and Hansen
- ▶ Ceramic structure (Diesel Particulate Filter)
 - ▶ Preliminary described by general damping



Simulation Setup

- ▶ Maximum element size = $\lambda/5 = 34$ mm
- ▶ 24.000 elements, 38.000 DOF
- ▶ PARDISO solver
- ▶ 100 discrete frequencies



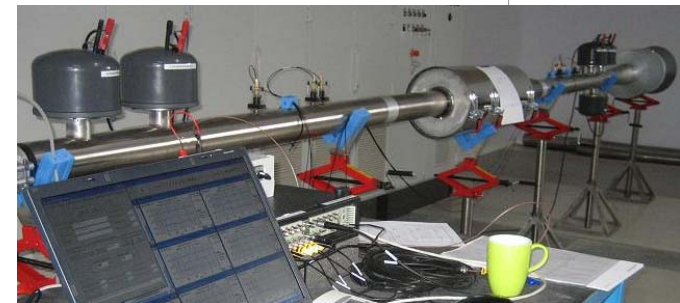
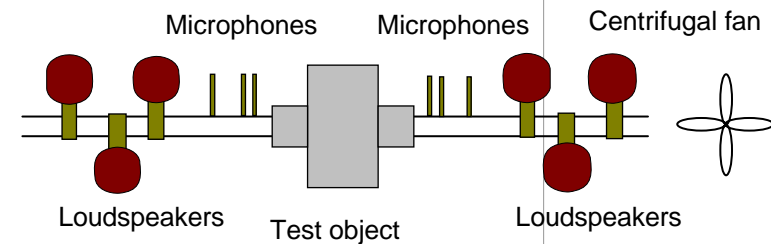
The Results



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The Measurement Setup

- ▶ The two source method
 - ▶ Up and down stream source direction
- ▶ Flow speed up to 30 m/s (cold air)
 - ▶ Corresponds to 160 kW engine @ rated speed



The Test Objects

- ▶ Reflection muffler
 - ▶ Simple expansion chamber
 - ▶ Quarter wave resonator
- ▶ Absorption muffler
- ▶ Perforated muffler
 - ▶ Hole size: $\text{Ø}3$, $\text{Ø}4$, $\text{Ø}8$, $\text{Ø}12$
 - ▶ Porosity: 10 – 40 %
- ▶ Automotive exhaust
 - ▶ Diesel Particulate Filter
 - ▶ Hybrid muffler



The reflection muffler



The absorption muffler



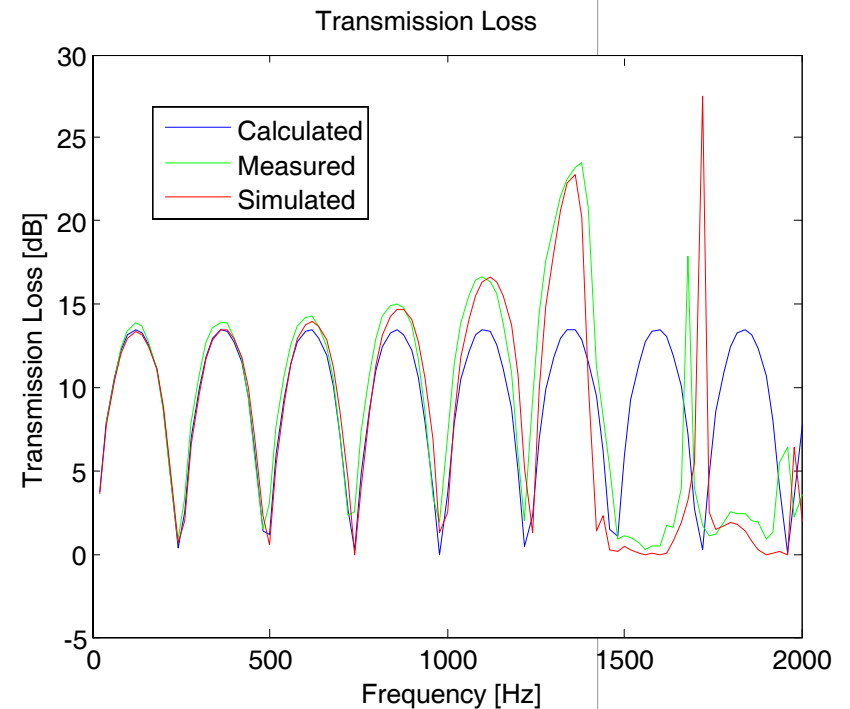
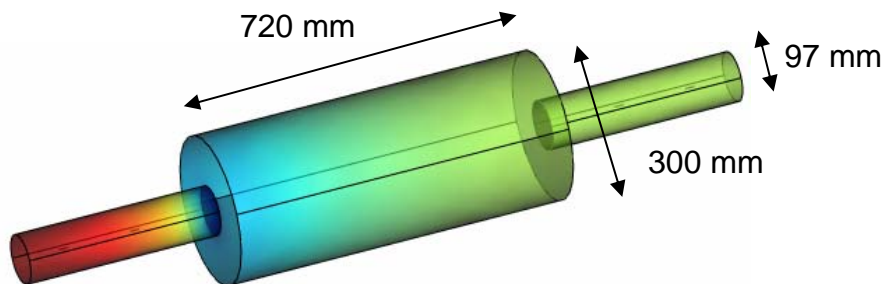
The perforated muffler



Automotive exhaust

The Reflective Muffler Comparison

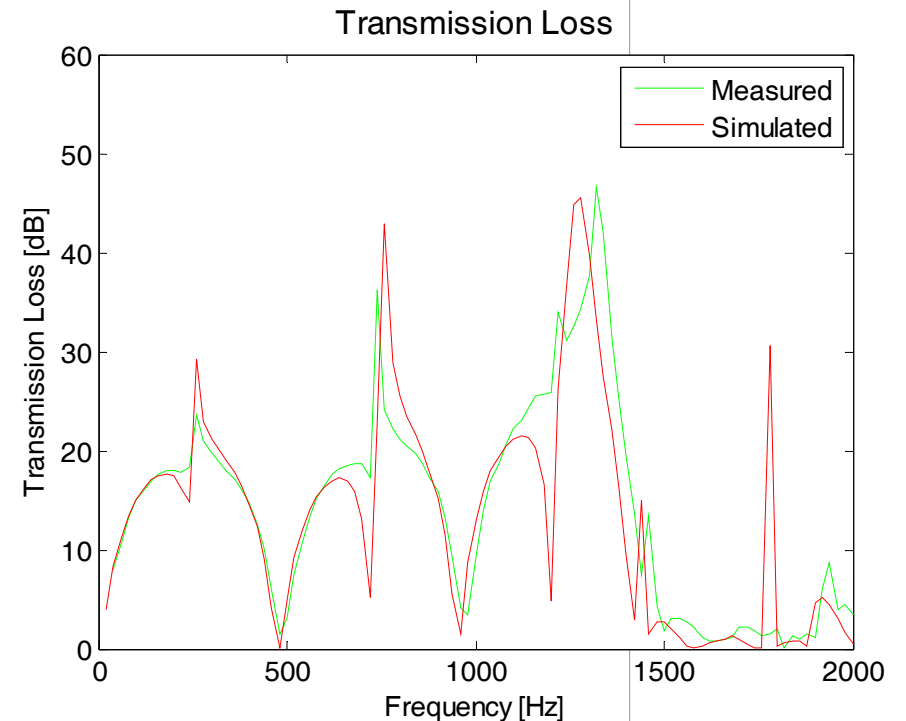
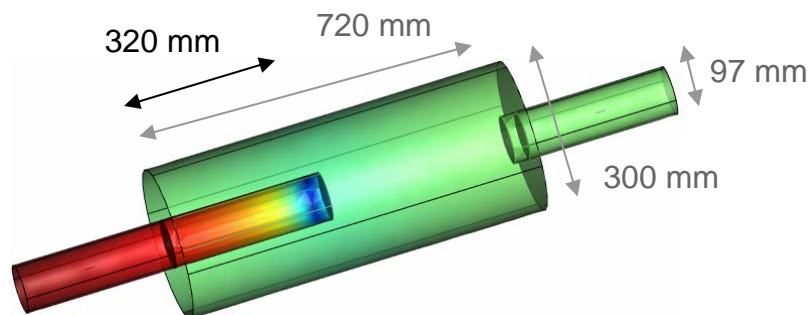
- ▶ Good correlation
- ▶ Peak offset due to inaccurate lengths, temperatures, densities
- ▶ First axisymmetric higher-order mode will propagate above 1400 Hz.
- ▶ First TL peak corresponds to a quarter muffler length



The Results

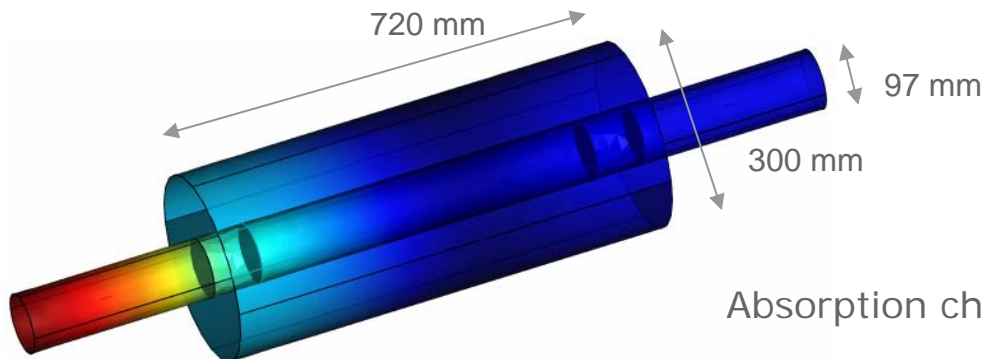
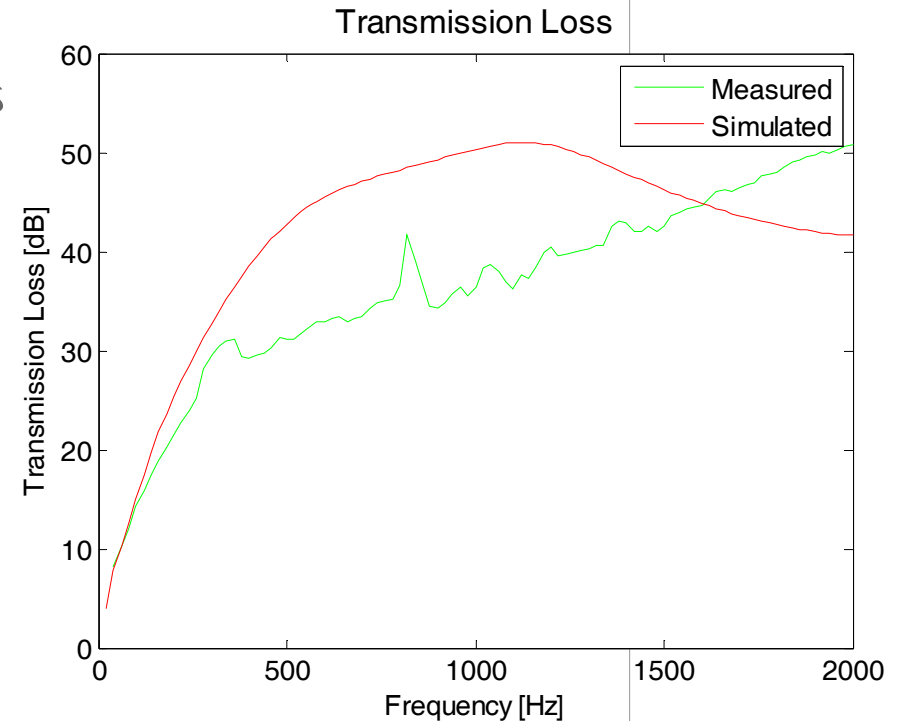
The Quarter Wave Resonator Comparison

- ▶ Again good correlation
- ▶ The first peak corresponds to a quarter pipe length.
- ▶ The 500 Hz minima could be eliminated by a pipe of 1/8 of the muffler length.



The Absorption Muffler Comparison

- ▶ Good low frequency correlation
- ▶ Mid & high frequency differences
 - ▶ Inaccurate Delany & Bazley model
 - ▶ Too large sub-domain



Absorption chamber – 5000 Rayls/m

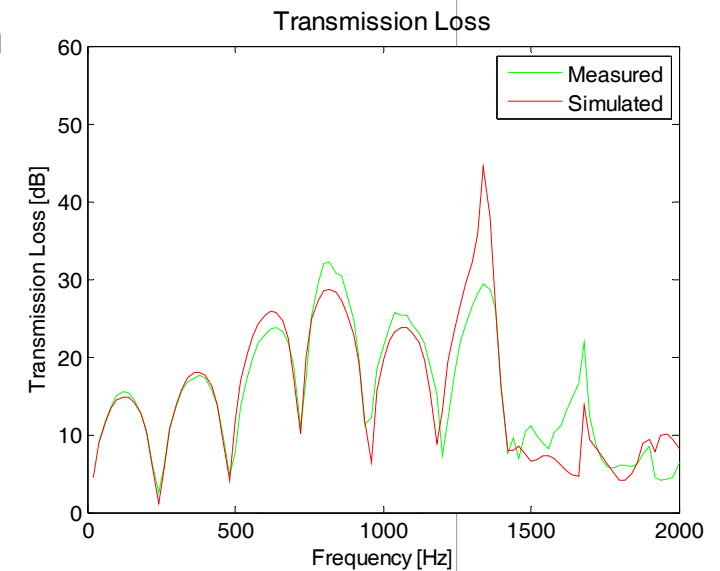
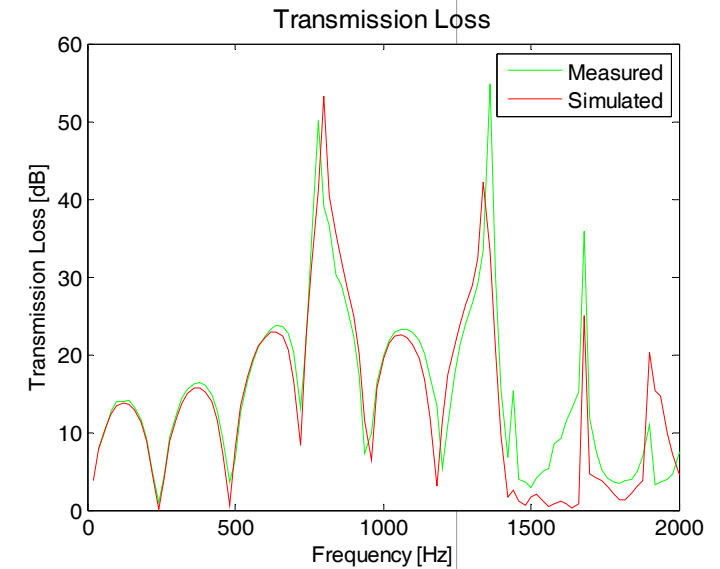
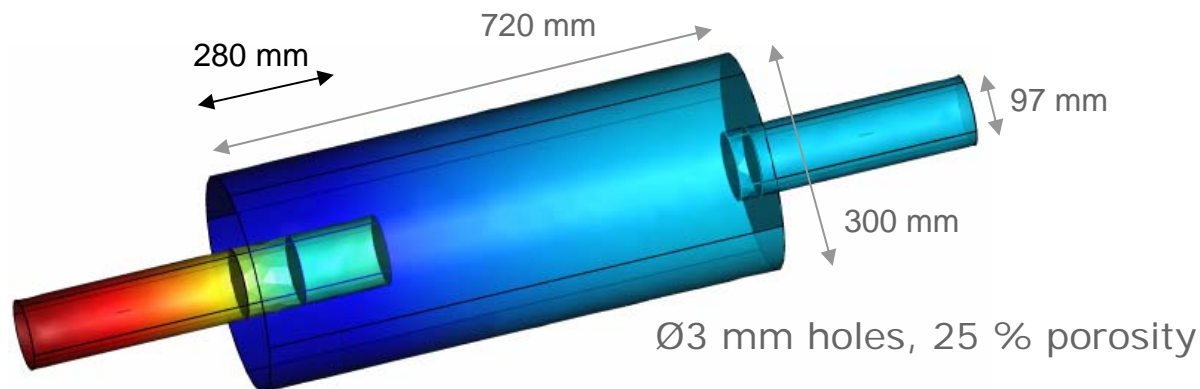


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The Results

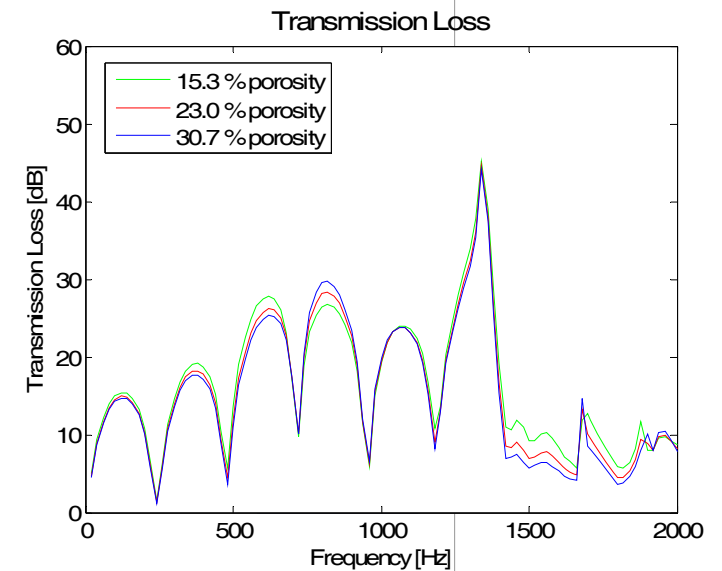
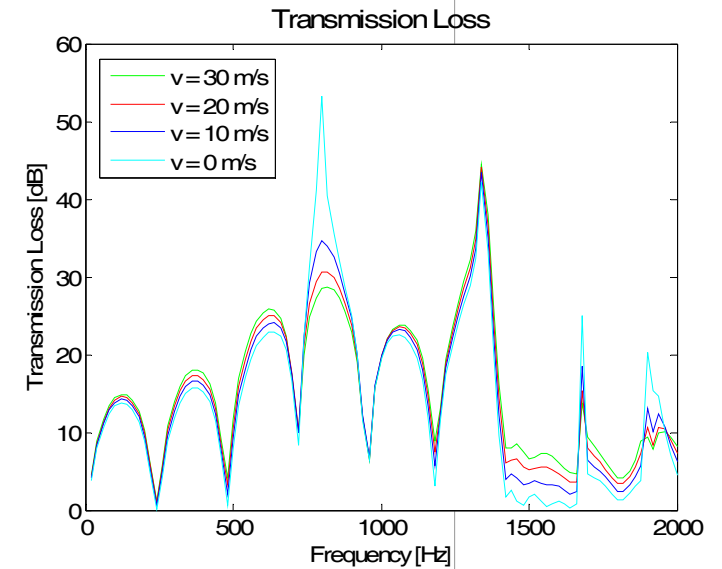
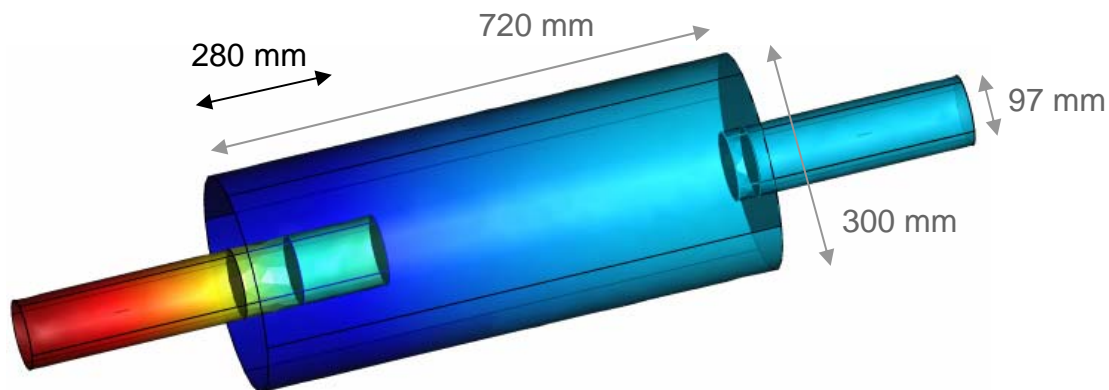
The Plug Flow Muffler Comparison

- ▶ 0 m/s flow speed
 - ▶ Good correlation
 - ▶ 800 Hz peak due to 80 mm extended inlet
- ▶ 30 m/s flowspeed
 - ▶ Good correlation
 - ▶ 1350 Hz peak not affected in simulation
 - ▶ Peaks limited by losses due to flow



The Plug Flow Muffler Simulations

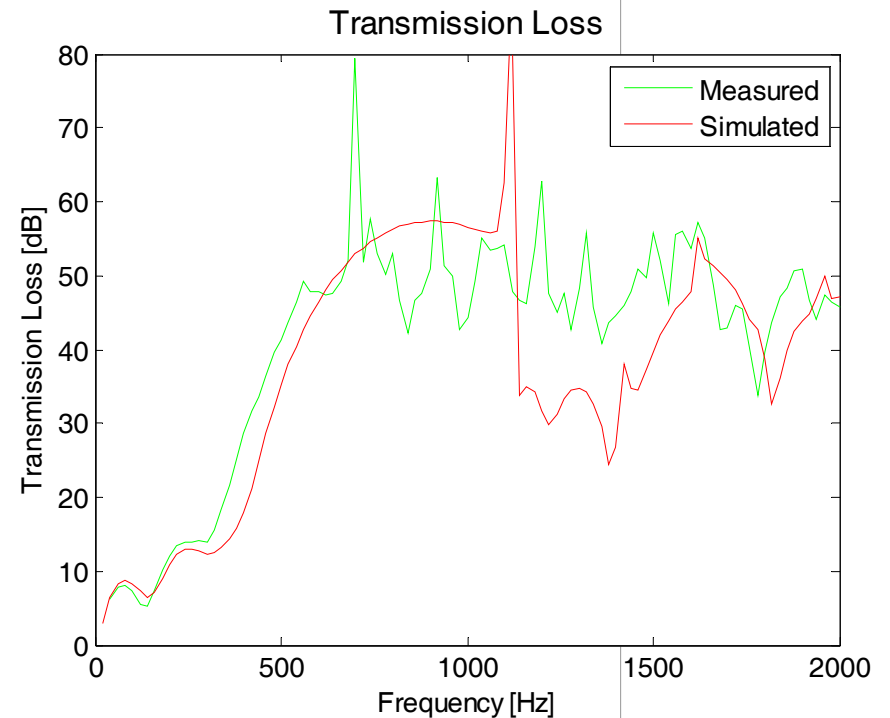
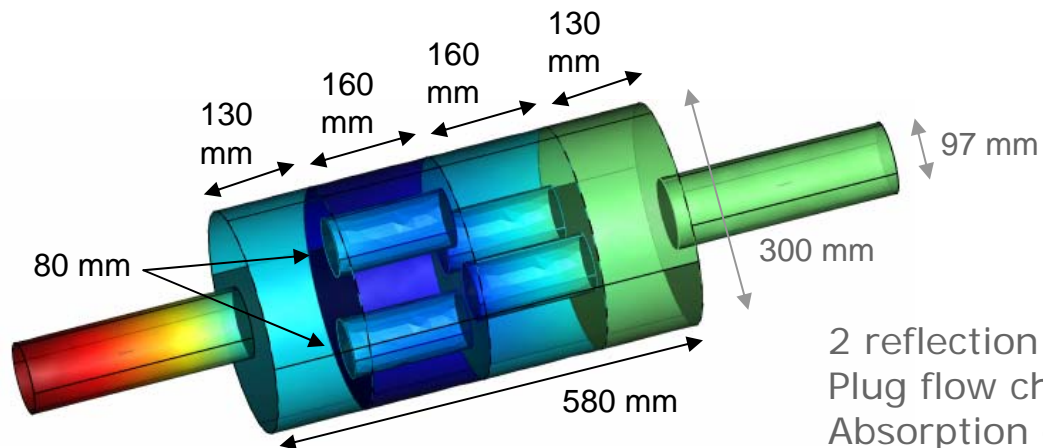
- ▶ Flow speed variations ($\Delta 3$, 25 %)
 - ▶ Flow smoothes the peaks and dips
- ▶ Porosity variations ($\Delta 4$, 30 m/s)
 - ▶ Same effect as changing the flow speed
 - ▶ Porosity is important, not hole size



The Hybrid Muffler

Comparison at 0 m/s

- ▶ Good correlation up to 700 Hz
- ▶ Difference due to
 - ▶ Inaccurate Delany & Bazley model
 - ▶ Slightly different lengths
 - ▶ Additional small features of in the real exhaust



2 reflection chambers
Plug flow chamber – $\text{Ø}3$, 30 %
Absorption chamber – 5000 Rayls/m



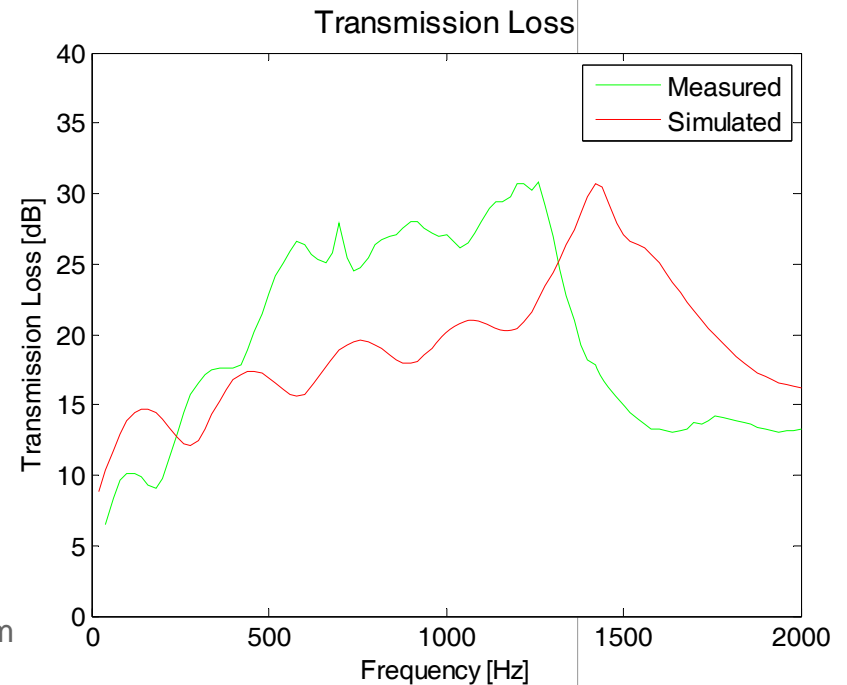
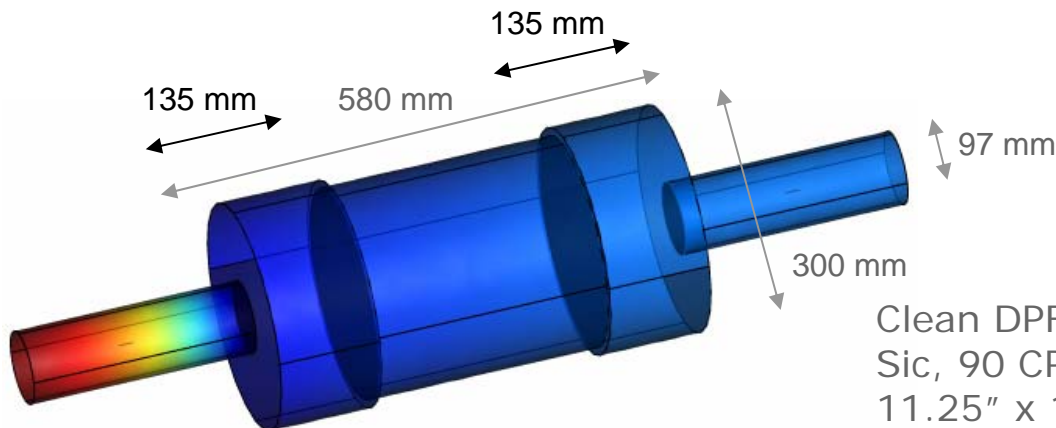
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The Results (preliminary)

The Diesel Particulate Filter

Comparison at 0 m/s

- ▶ No correlation (general damping)
- ▶ Additional simulations proved the model against measurements made by KTH



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Conclusion

- ▶ Successful transfer matrix approach
 - ▶ One run
 - ▶ Insertion loss calculation possible
- ▶ Model validation
 - ▶ Reflective and plug flow muffler
 - ▶ Absorptive and ceramic
- ▶ Simulation approach
 - ▶ Frequency limitations by pipe diameter
 - ▶ Short setup time
 - ▶ Easy redesign



Future work

- ▶ Pressure loss and mean flow distribution simulation
-> backpressure result
- ▶ Source impedance measurements
-> Insertion loss results



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Questions?



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Appendix



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Benefits

- ▶ Of acoustic simulation of exhaust systems
 - ▶ Reduced cost price and development time
 - ▶ Increased performance and knowledge
 - ▶ Minimizing material consumption
 - ▶ Simplifying construction and production

- ▶ Of using the Transfer Matrix approach
 - ▶ Modular approach
 - ▶ Transmission loss calculation
 - ▶ Insertion loss calculation



Limitations

- ▶ Upper frequency is 2 kHz $f < \frac{1.84c}{\pi D}$
 - ▶ D is the duct diameter
 - ▶ f is the frequency
 - ▶ c is the speed of sound
- ▶ Exhaust system length max 15 m
- ▶ Max 150 dB re 20 μ Pa
- ▶ Constant temperature
- ▶ Zero mach number