

# Computational Modeling of Synthetic Jets

David Durán

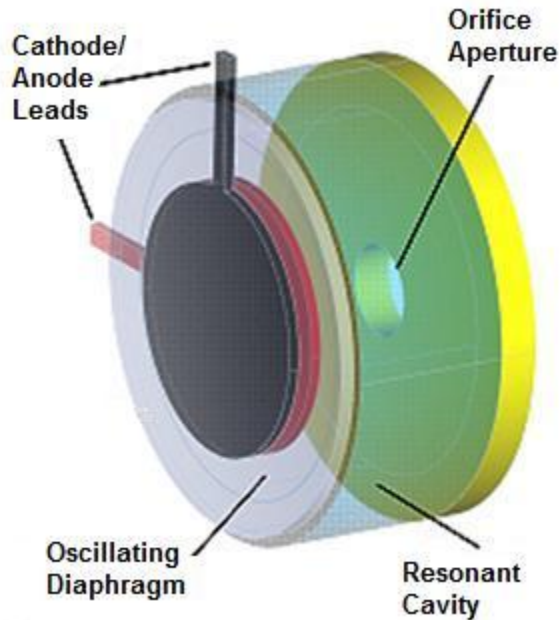
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**Comsol Conference 2010 – Boston, October 7-9**

1. Motivation
2. Methodology
3. Dimensional analysis of the problem
4. 3D Piezoelectric Disk Model
5. Axisymmetric SJ Actuator Model
6. Numerical Results
7. Conclusions
8. Contact
9. References



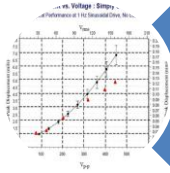
Tridimensional Schematic of the Synthetic Jet Actuator.  
Image from (Morpheus Laboratory, University of Maryland,  
2009)

## Applications

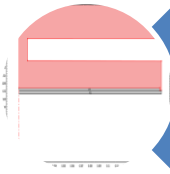
- Separation Control
- Flow Control
- Mixing
- Heat Transfer

## Why Comsol?

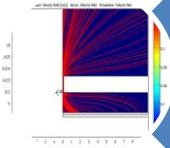
- Multiphysics Problem
- Other simulations only include Navier-Stokes



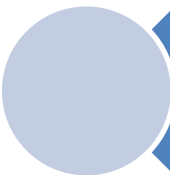
## 1. Validation of the Disk 3-D Model



## 2. Axisymmetric Model



## 3. Analysis of the Relevant Dimensionless Numbers according to different parameters of the model



## 4. Conclusions

- The vortex ring formation depends on the velocity field of the fluid at the aperture of the Actuator
- The average velocity cannot be the characteristic velocity because it is zero
- Max. Velocity ( $U$ ) was chosen as the characteristic velocity.

$$U = f(d, \nu, \omega)$$

- Since there are 4 variables and 2 dimensions, the problem can be described with 2 non dimensional numbers

Reynolds Number

$$Re = \frac{Ud}{\nu}$$

Stokes Number

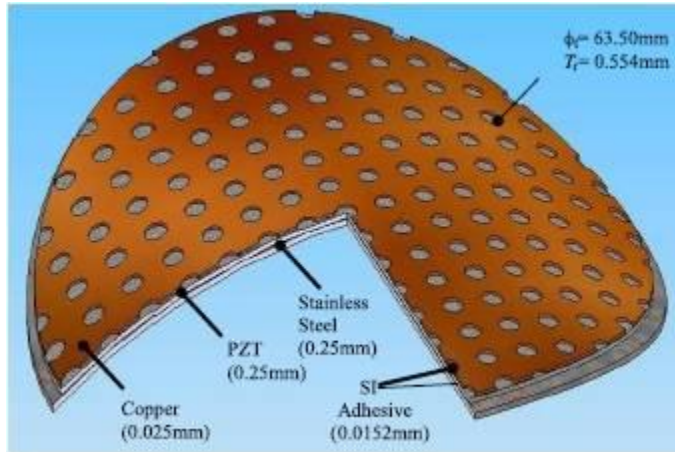
$$S = \sqrt{\frac{\omega d^2}{\nu}}$$

These two numbers be related through the Inverse of the Strouhal Number:

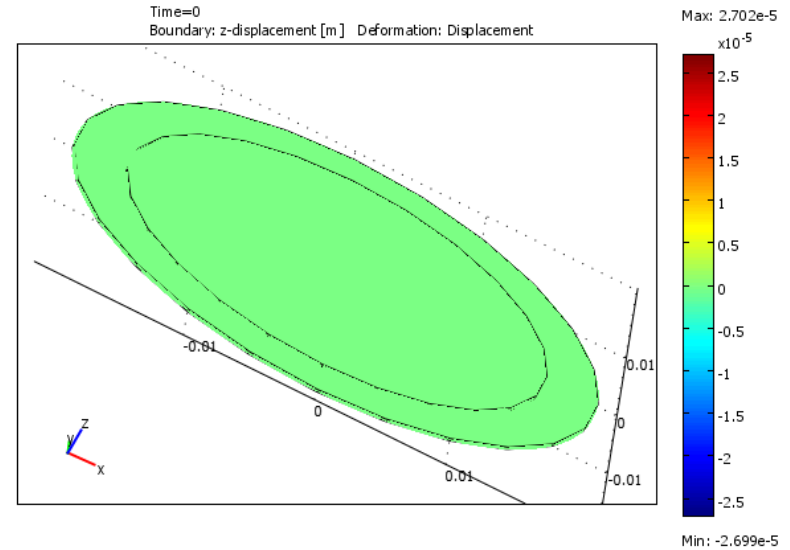
$$\frac{1}{Sr} = \frac{Re}{S^2}$$

According to Holman et al. 2005, the criterion of formation for synthetic jets can be defined as follows:

$$\text{If } \frac{1}{Sr} > C \rightarrow \text{jet}$$



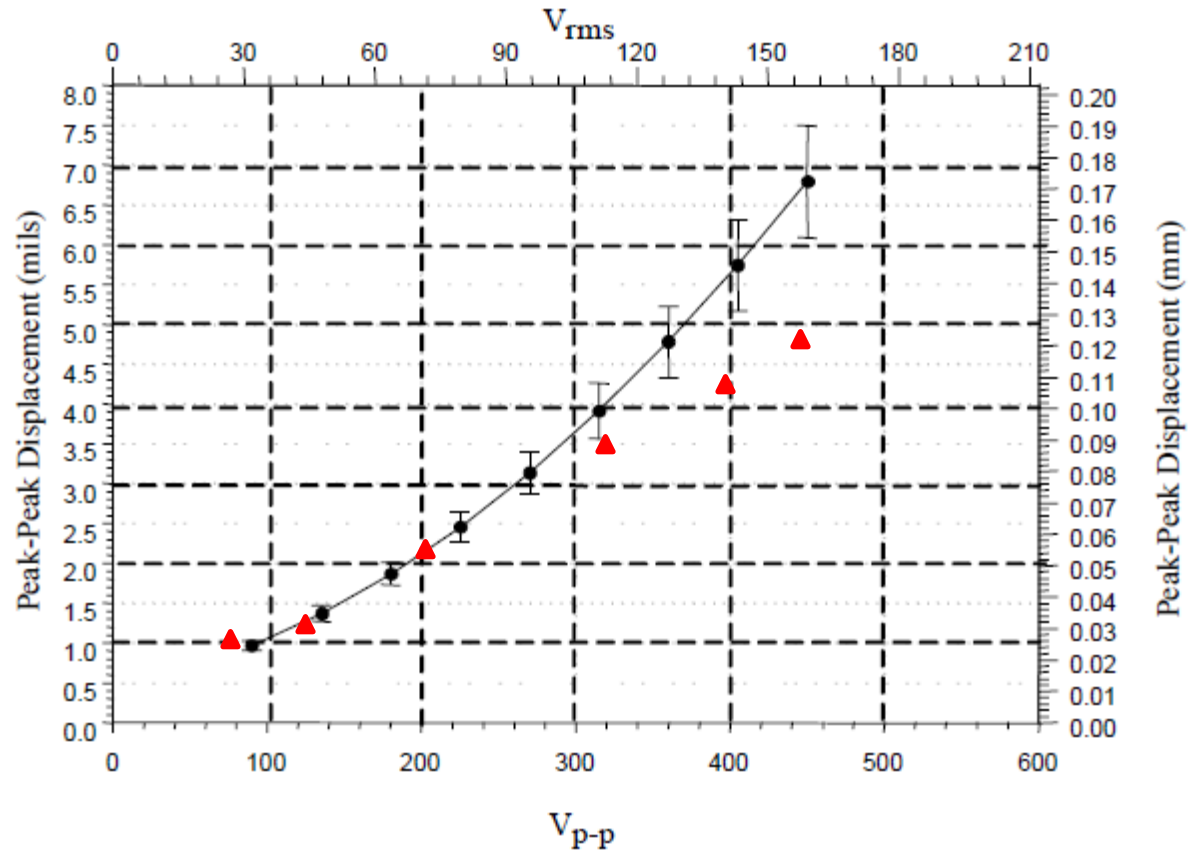
Schematic of the piezoelectric diaphragm showing all the components of the same. Image from (Mane, Mossi, & Bryant, 2008)



3D Model of the Disk in Comsol 3.4

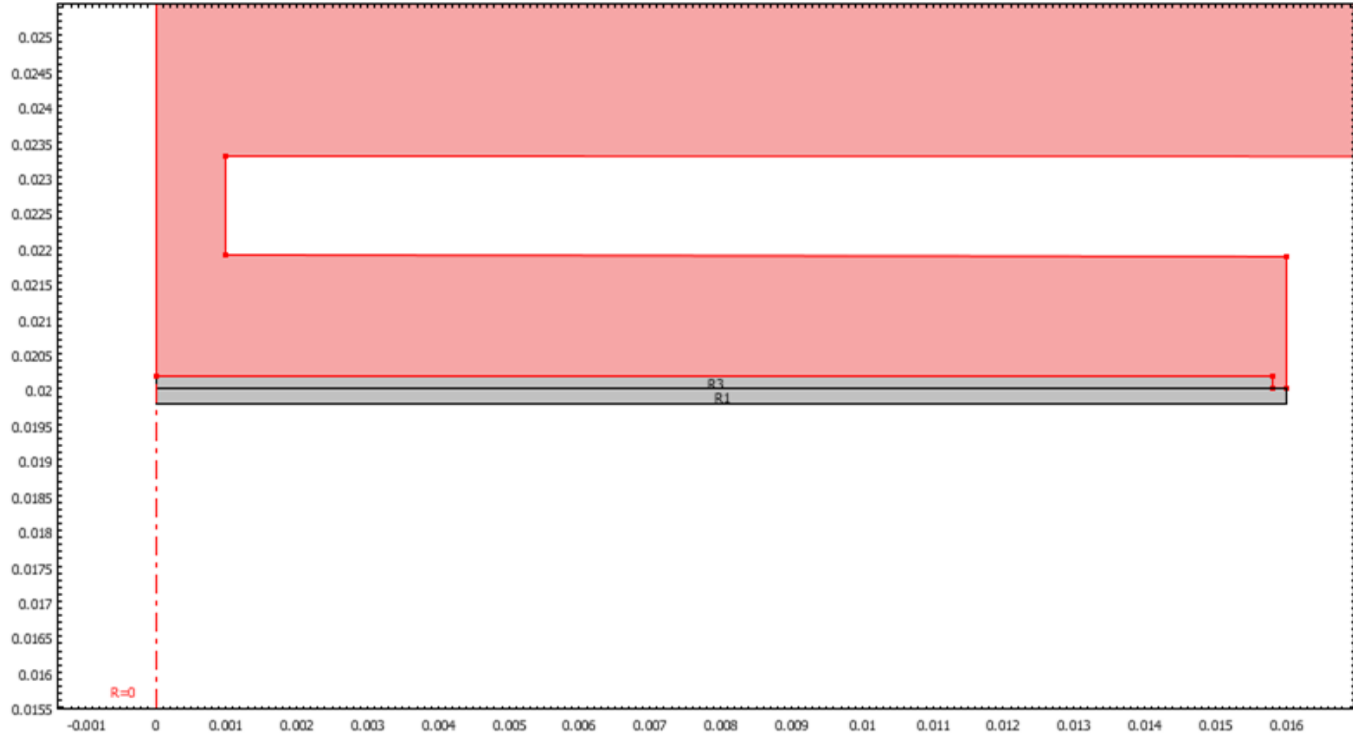
## Displacement vs. Voltage : Simply Supported

Typical Performance at 1 Hz Sinusoidal Drive, No Load

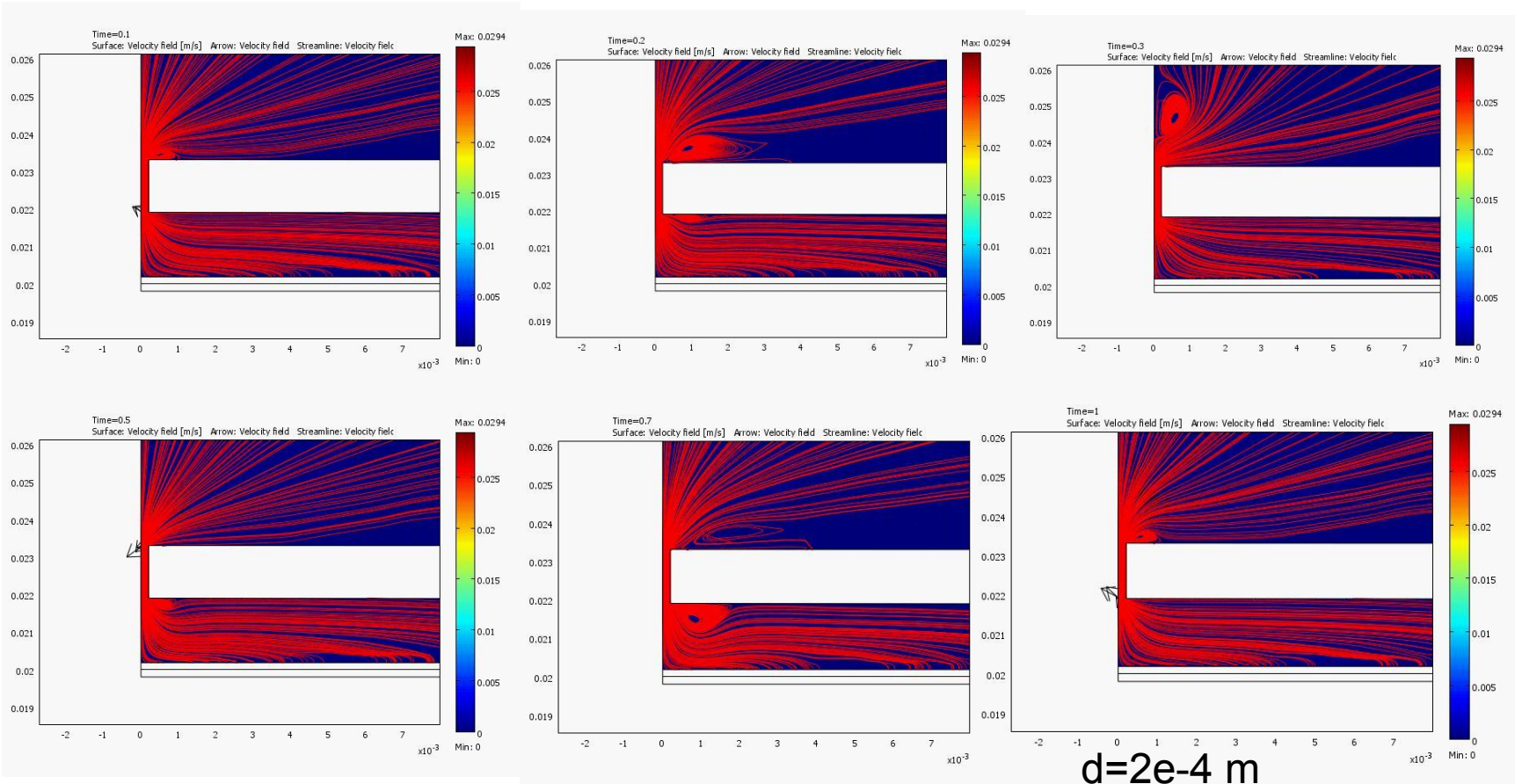


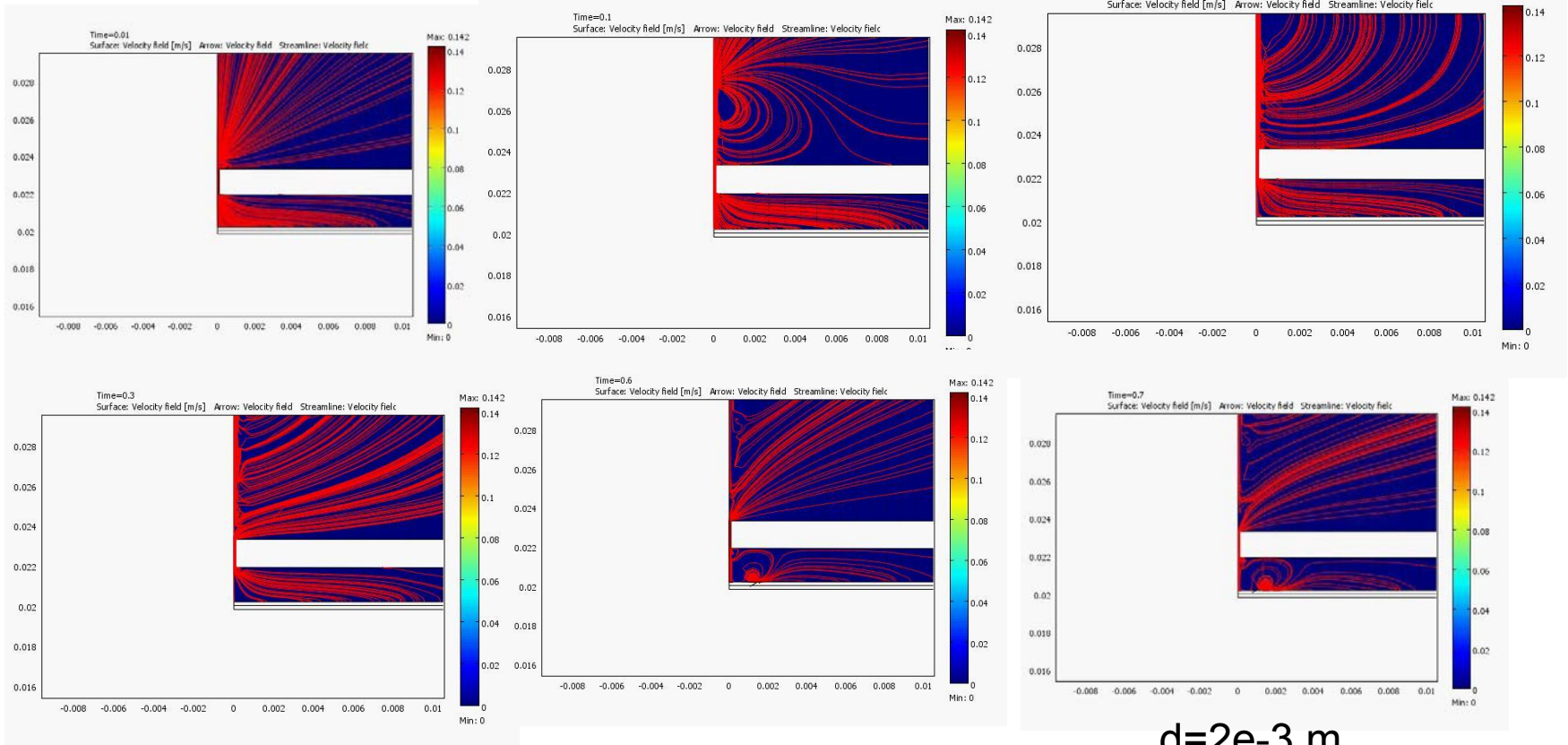
The graph in black is from the Datasheet of THUNDER. Manufactured by FACE International





Exp. No.	Diam. (m)	height (m)	Potential (V)	viscosity (Pa.s)	Vel max. (m/s)	Reynolds	Stokes	1/Sr	Criterion
<u>1</u>	2e-03	1.4e-03	25	1e-06	3.27e-03	6.54	5.01	0.26	no jet
<u>2</u>	2e-03	1.4e-03	50	1e-06	3.27e-03	6.54	5.01	0.26	no jet
<u>3</u>	2e-03	1.4e-03	200	1e-06	3.02e-03	6.05	5.01	0.24	no jet
<u>4</u>	2e-04	1.4e-03	100	1e-06	1.21e-01	24.2	0.50	96.29	no jet
<u>5</u>	2e-04	1.4e-03	500	1e-06	1.21e-01	24.2	0.50	96.29	no jet
<u>6</u>	2e-04	1.4e-03	100	1e-07	0.135	270	1.59	107.43	jet
<u>7</u>	2e-04	1.4e-03	100	1e-06	0.146	29.2	0.50	116.18	jet


 $d=2e-4 \text{ m}$ 
 $V=100 \text{ V}$ 
 $f=1 \text{ Hz}$ 
 $\nu=1e-6 \text{ Pa.s}$ 
 $\text{density}=1 \text{ kg/m}^3$ 
 $1/\text{Sr}=96.29$


 $d=2e-3 \text{ m}$ 
 $V=100 \text{ V}$ 
 $f=1 \text{ Hz}$ 
 $\nu=1e-9 \text{ Pa}\cdot\text{s}$ 
 $\rho=1 \text{ kg/m}^3$ 
 $1/\text{Sr}=107.43$

- The fluid velocity is weakly dependant of the applied voltage
- The fluid velocity is strongly dependant of the aperture diaphragm
- The jet formation criterion is in the order of hundreds
- There exists vortex ring formation in the inside of the cavity

- Study of the influence of other geometric parameters such as: actuator's height, Disk diameter, etc
- Study of the influence of the frequency in the SJ formation
- Coupling of the acoustics module
- Comparison with the Lumped Element Model
- Study of the influence of the vortex rings interactions with the diaphragm in the quality of SJ formation

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