

JOULE HEATING EFFECTS ON ELECTROOSMOTIC FLOW OCCURRING IN A CYLINDRICAL CONSTRICTION MICROCHANNEL

Presentation By

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**COMSOL
CONFERENCE
BANGALORE2013**

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Introduction

- Microfluidics deals with the precise control and manipulation of fluids and particles which are constrained to a micro scale.
- With the advent of easy micro-fabrication techniques, there has been an increasing development in the lab-on-a-chip (LOC) devices.
- A lab-on-a-chip is a device that integrates several laboratory functions into a single chip of centimeters in size

Electro kinetic Phenomenon

- Application of electric fields along the microchannel controls the movement of bulk fluid and the particles
- three important phenomenon are
 - Electro-osmosis
 - Electrophoresis.
 - Dielectrophoresis .
- These phenomena are used in the microfluidics to manipulate particles and cells like focusing, trapping and separating them.

Concept of Joule Heating

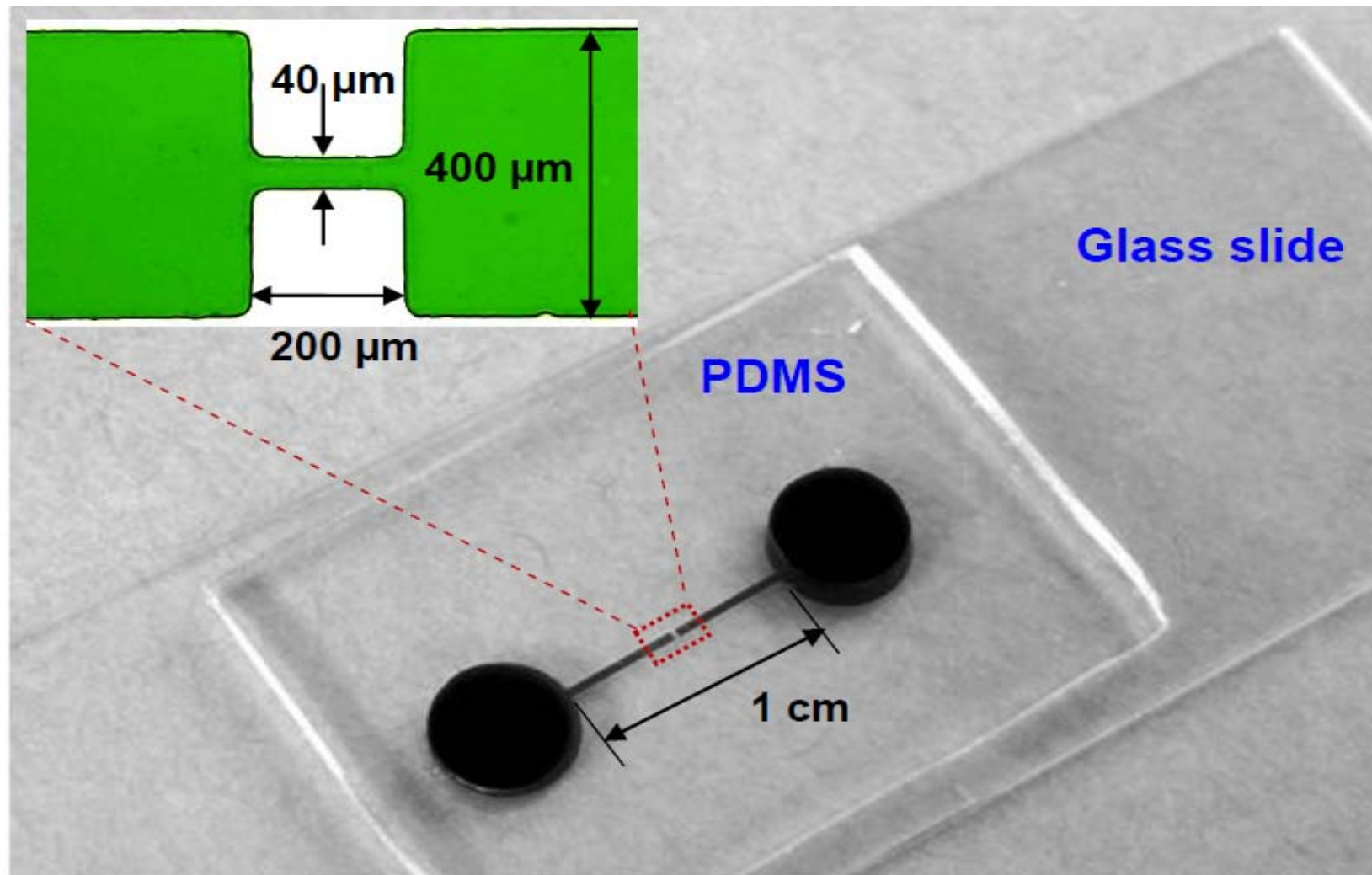
- When a wire is immersed in a mass of water and electric current is applied temperature of the water increased due to the current flowing through the wire for a considerable length of time.
- When voltage difference is applied at the electrodes, electric energy is consumed by resistive fluid as electric current flow through and transformed into heat.

- Heat generated due to joule heating is proportional to the square of electric field

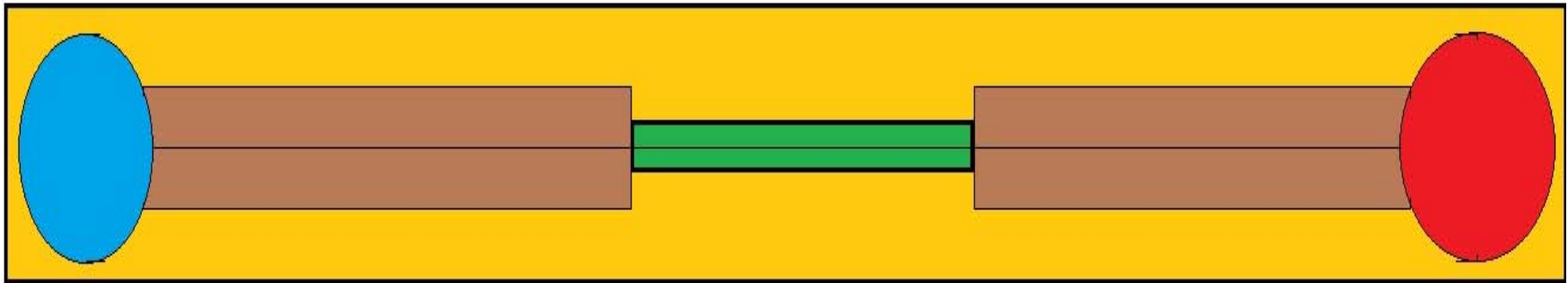
$$Q = \sigma(\mathbf{E} \cdot \mathbf{E})$$

- Where Q is the heat generated in W/m³, σ is the electrical conductivity in S/m and E is the electric field in V/m.

Problem Setup (Sriram Sridharan)



Problem definition

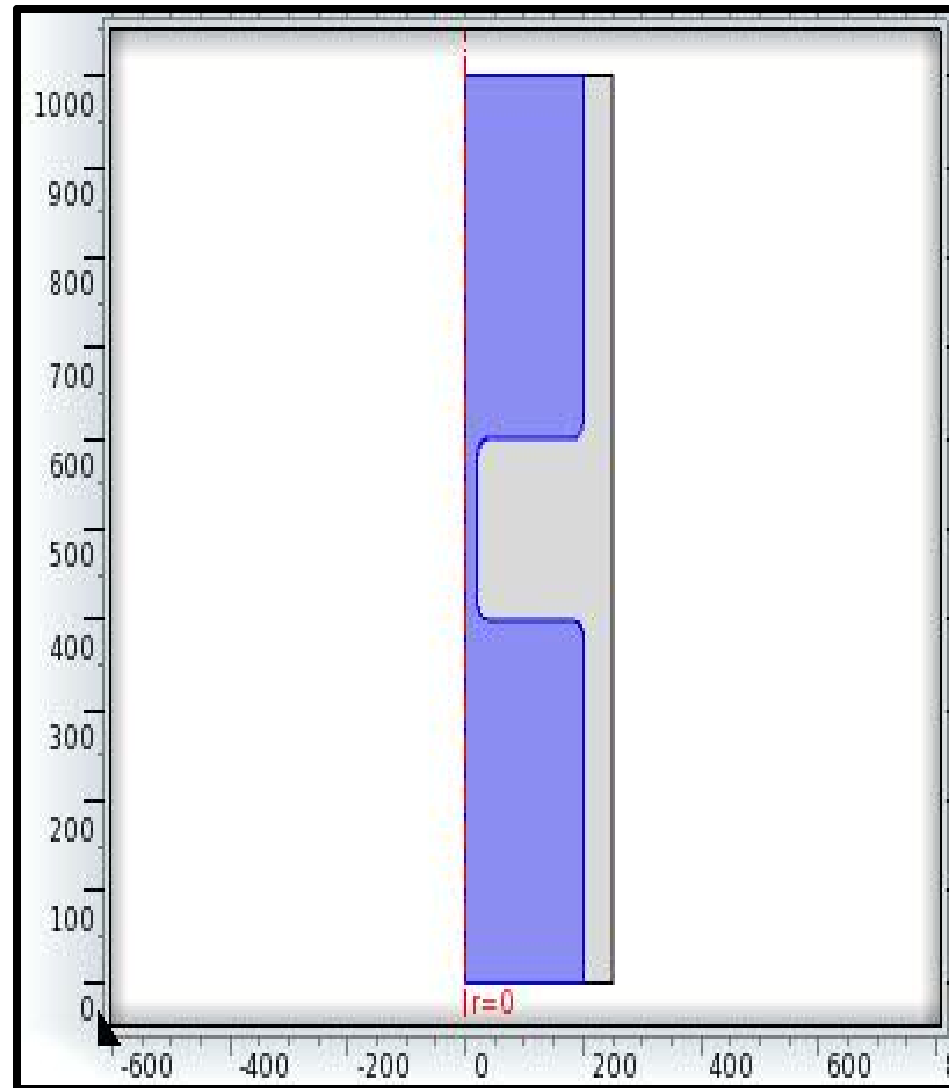


Geometry

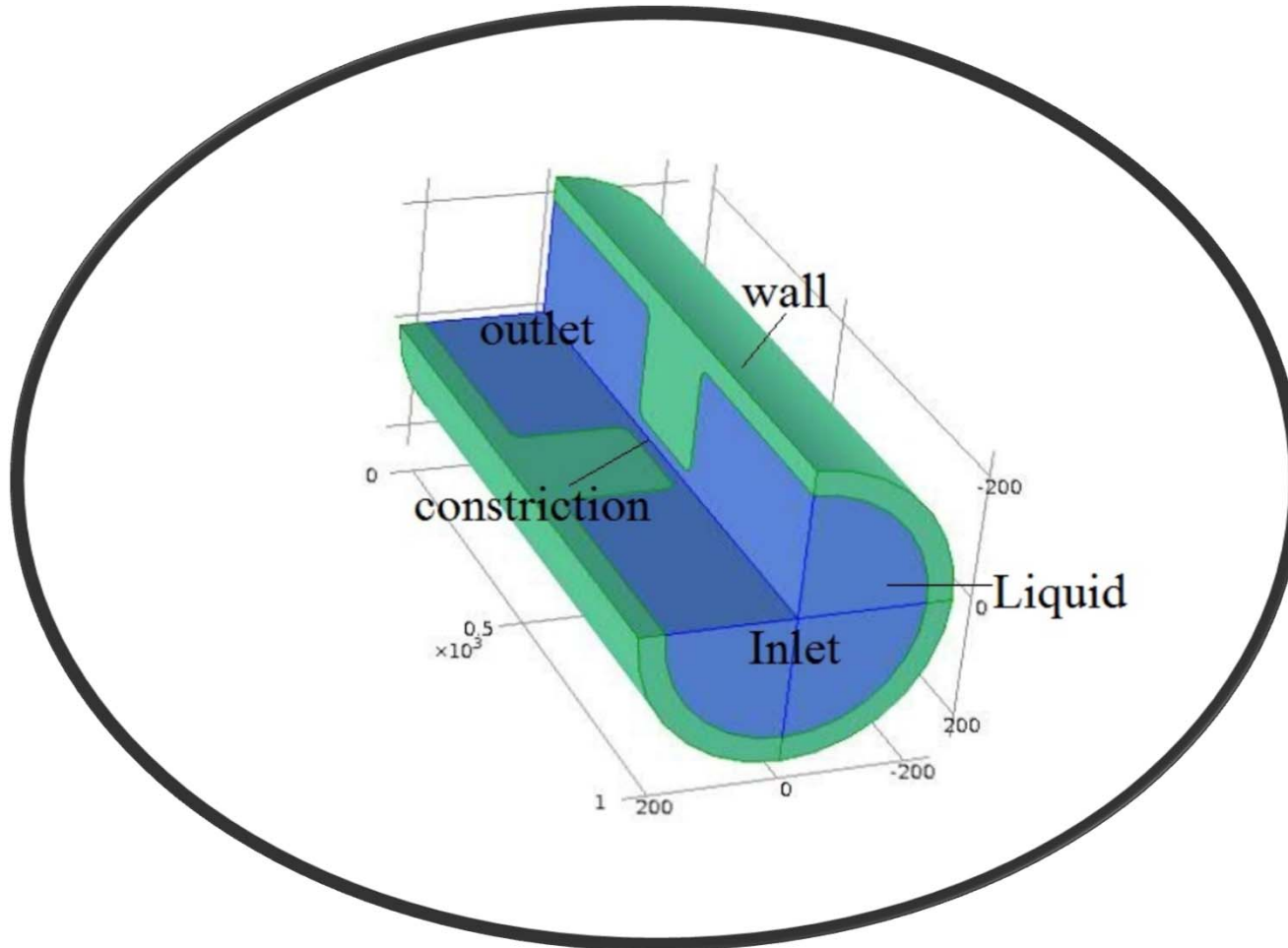
Top View

Zoomed in View

- Axisymmetry
- Length 1000 μm .
- Outer radius 250 μm .
- Inner radius 200 μm .
- Constriction length 200 μm .
- Constriction radius 20 μm .



Exploded View



Physics Used for simulation

- Ac/Dc Module - Electric currents (dc)
- Heat transfer Module – Conjugate heat transfer (Laminar flow)

Basic Equations used

1. $\nabla \cdot (\sigma \nabla \phi) = 0$

2. $\rho C_p u \nabla T = \nabla \cdot (K \nabla T) + Q$

$$Q = \sigma E^2 \text{ (W/m}^3 \text{)}$$

$$\nabla \cdot (K_p \nabla T) = 0$$

$$3. \quad \nabla \cdot \mathbf{V} = 0$$

$$\rho(\mathbf{V} \cdot \nabla)\mathbf{V} = -\nabla p + \nabla \cdot (\mu \nabla \mathbf{V}) + \rho_e \mathbf{E}$$

Electro osmotic velocity

$$u_{eo} = \mu_{eo} \mathbf{E} \quad (\text{m/s}) \quad (\text{Helmholtz-Smoluchowski Eqn})$$

$$\mu_{eo} = \varepsilon_0 \varepsilon_r \frac{\zeta}{\mu} \quad (\text{m}^2/\text{V.s})$$

COMSOL Implementation

- 2D Axisymmetry
- Physics
- Geometry Building
- Material Selection
- Boundary Condition
- Meshing
- Post Processing

Boundary Conditions

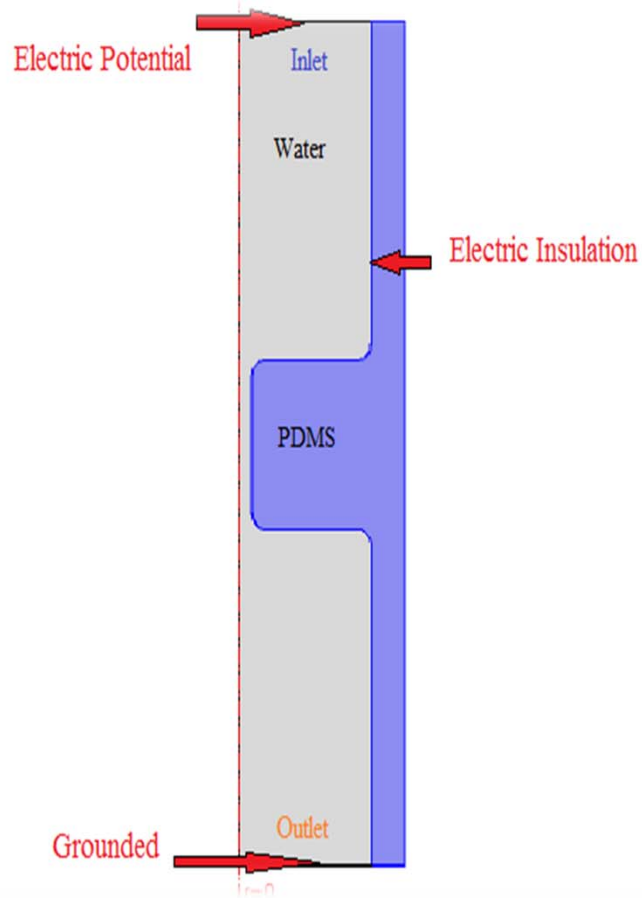


Figure Electric Boundary Condition

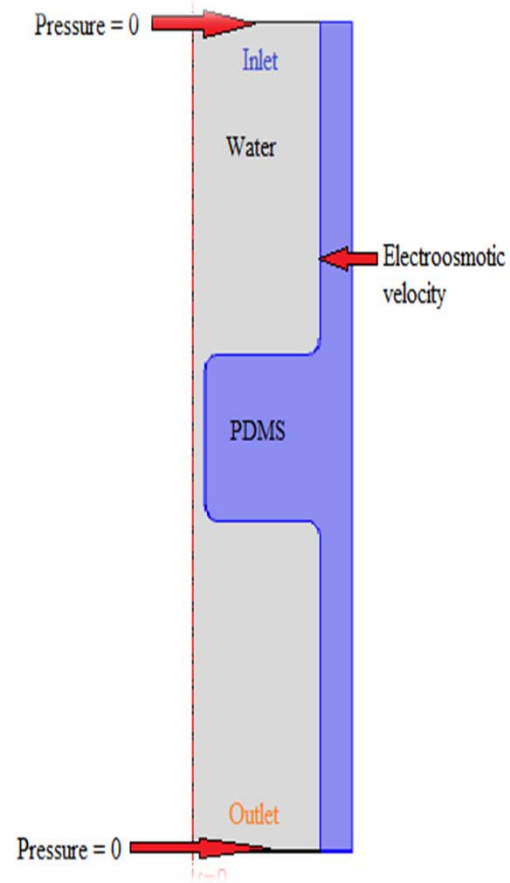
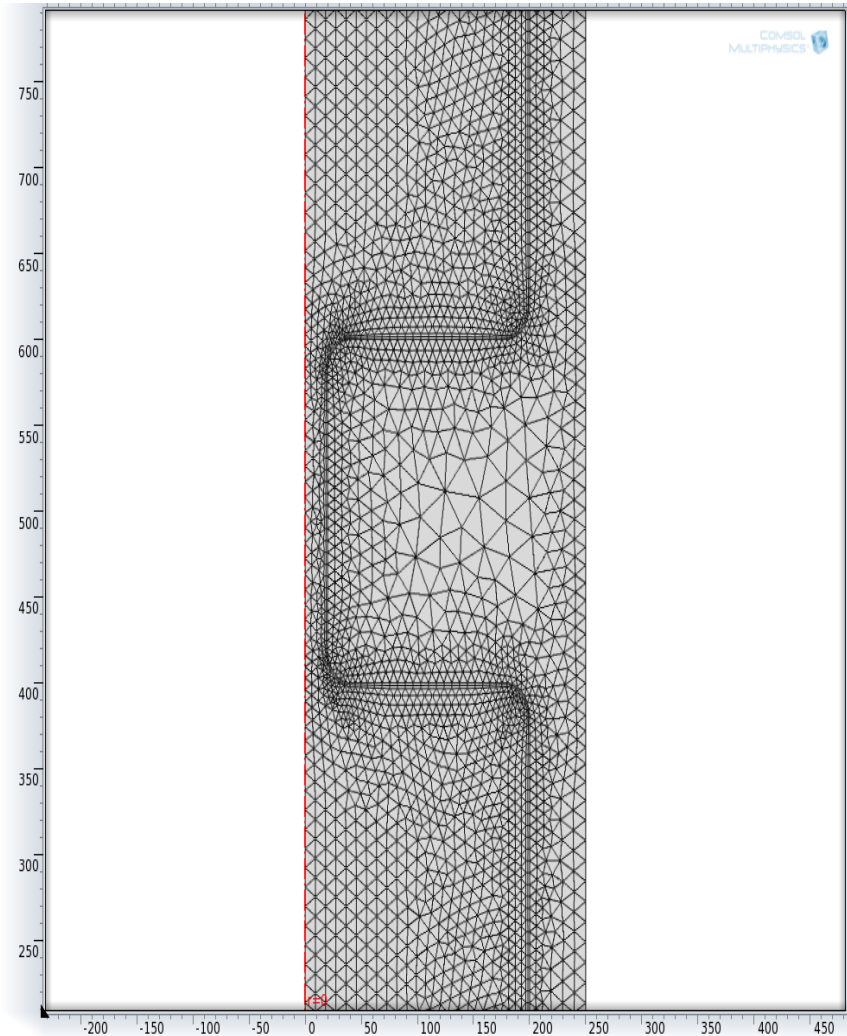


Figure: Flow Boundary Condition

Meshing

- The mesh consists of around 7109 triangular elements and about 418 quadrilateral elements
- Average mesh quality of 0.94.



Results

- How Joule heating effects the velocity profile?
- How velocity profile was altered due to Joule heating?
- Comparison of velocity profile with and without Joule heating.

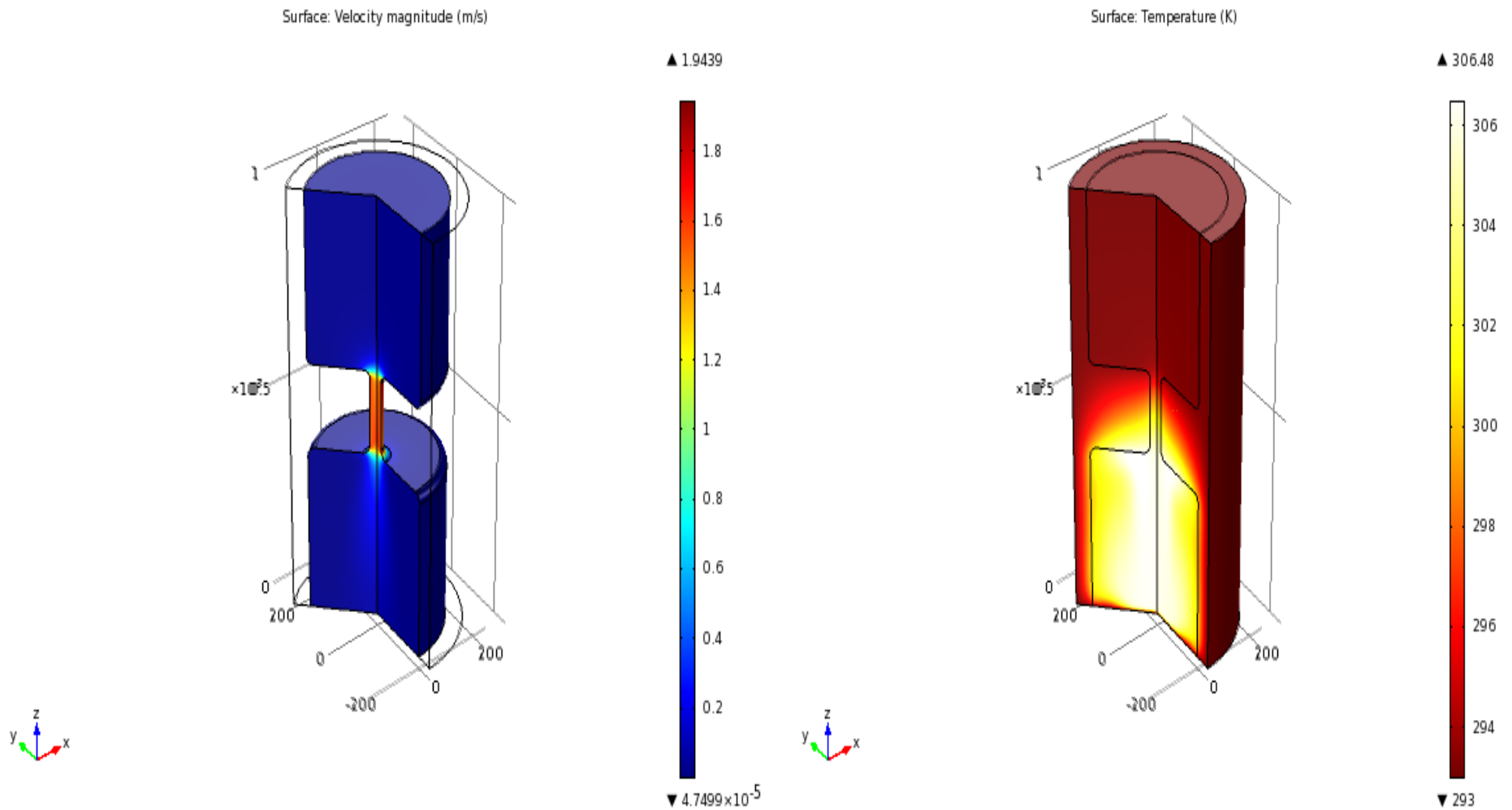


Figure : Velocity and Temperature distribution of a cylindrical microchannel with zeta potential -10 mV

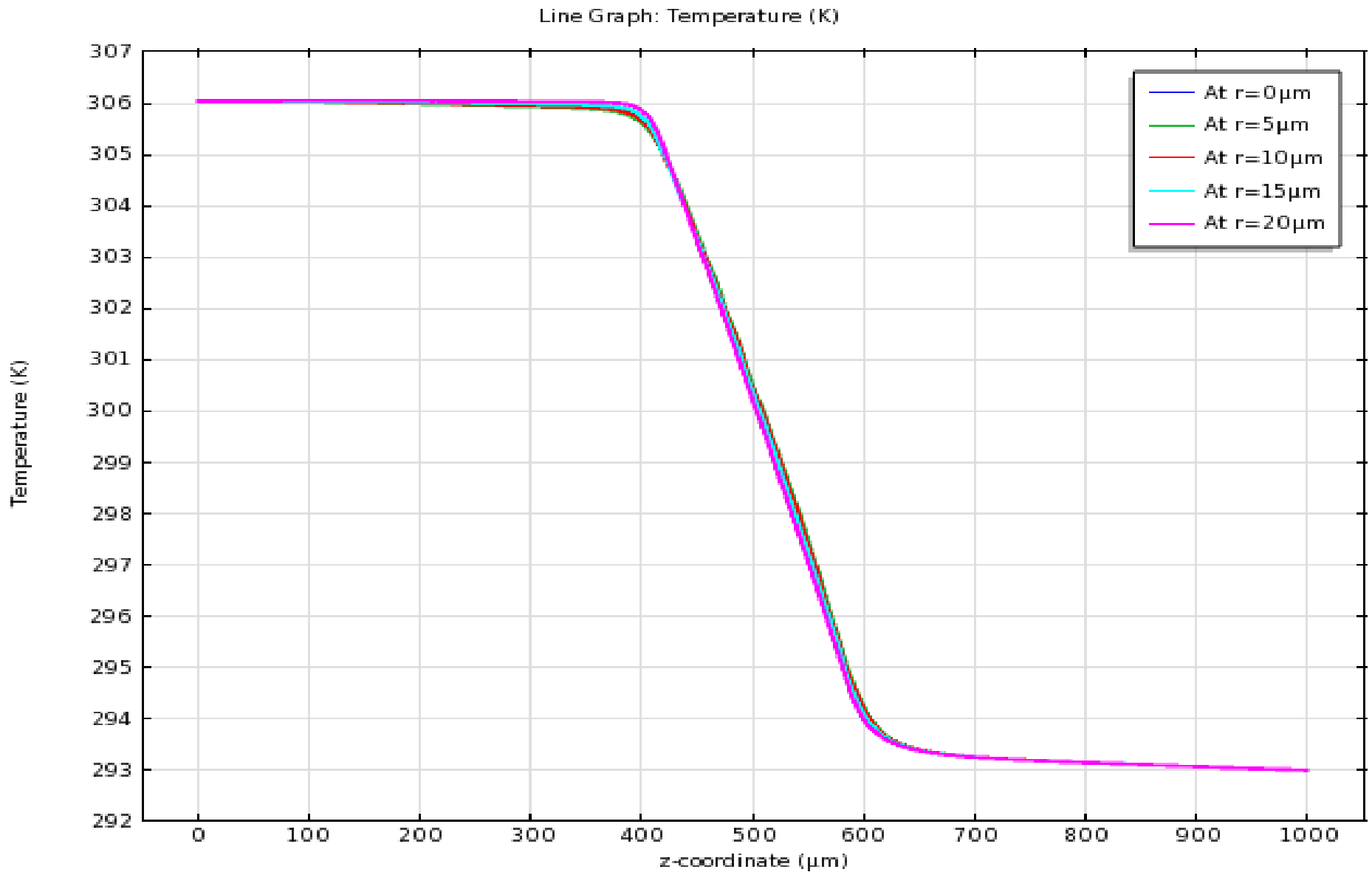


Figure : Temperature profile along a cylindrical microchannel with zeta potential of -10 mV

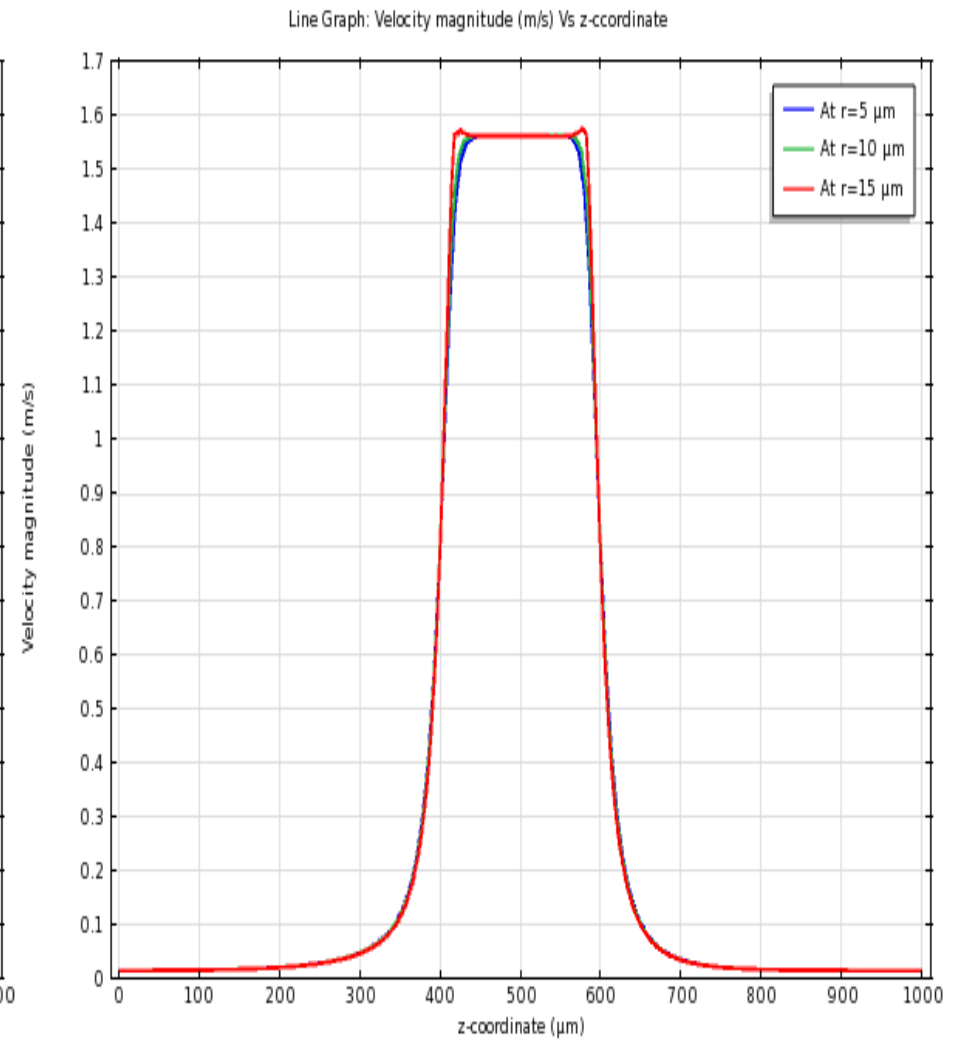
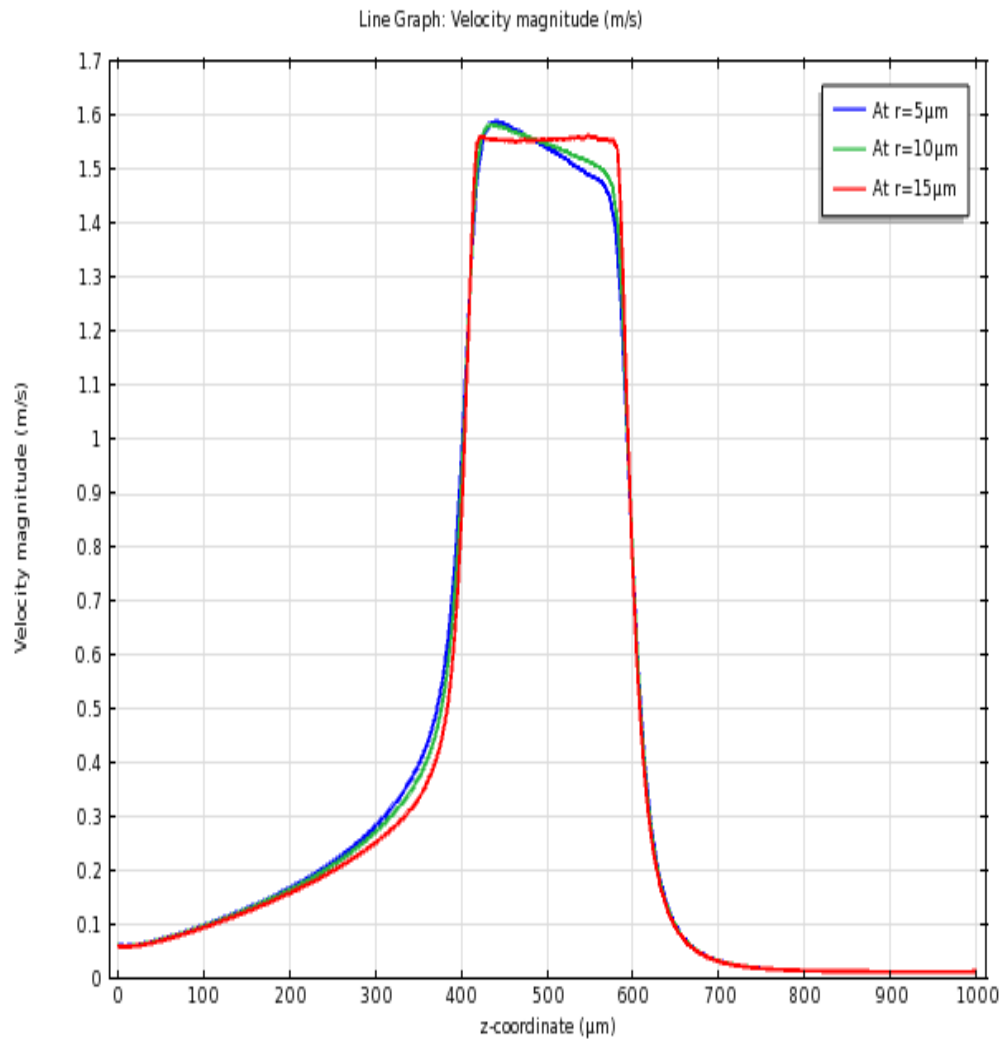


Figure : Velocity profile along a cylindrical microchannel with and without Joule heating

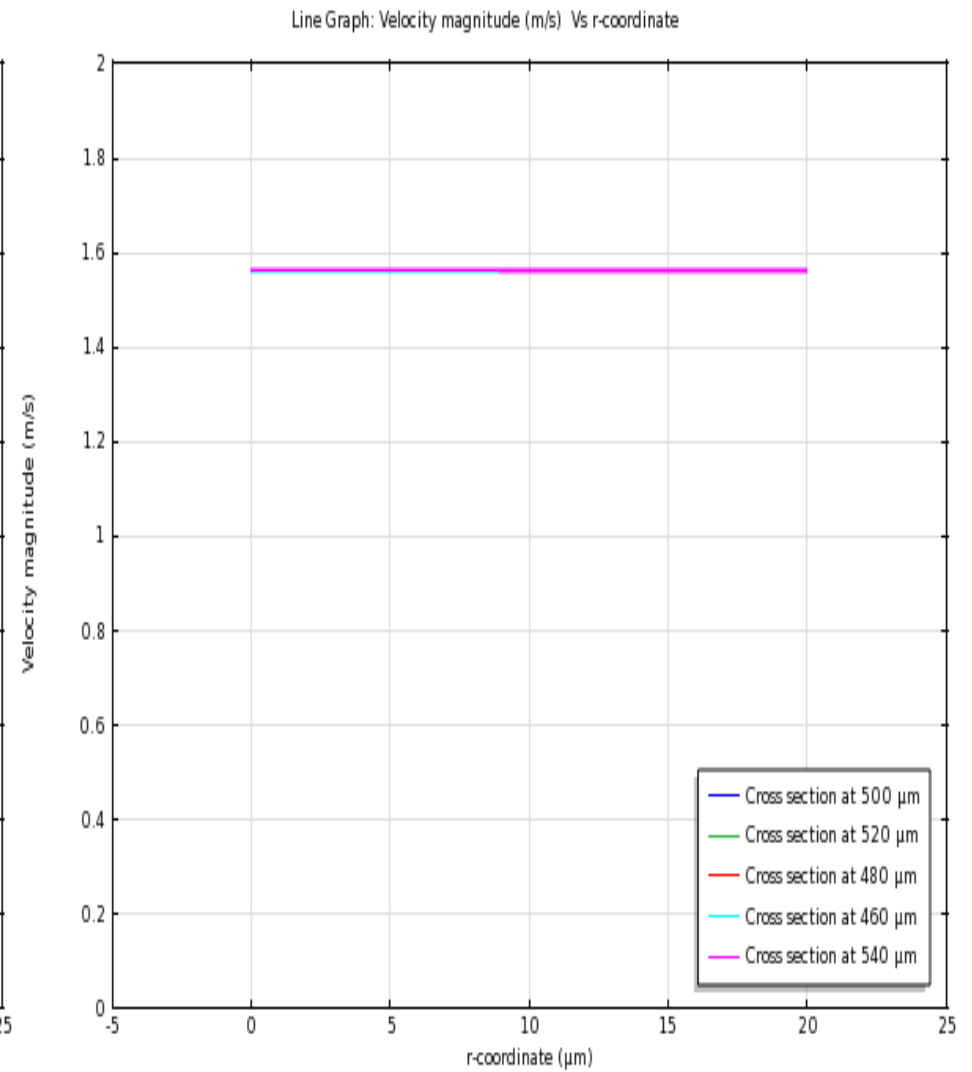
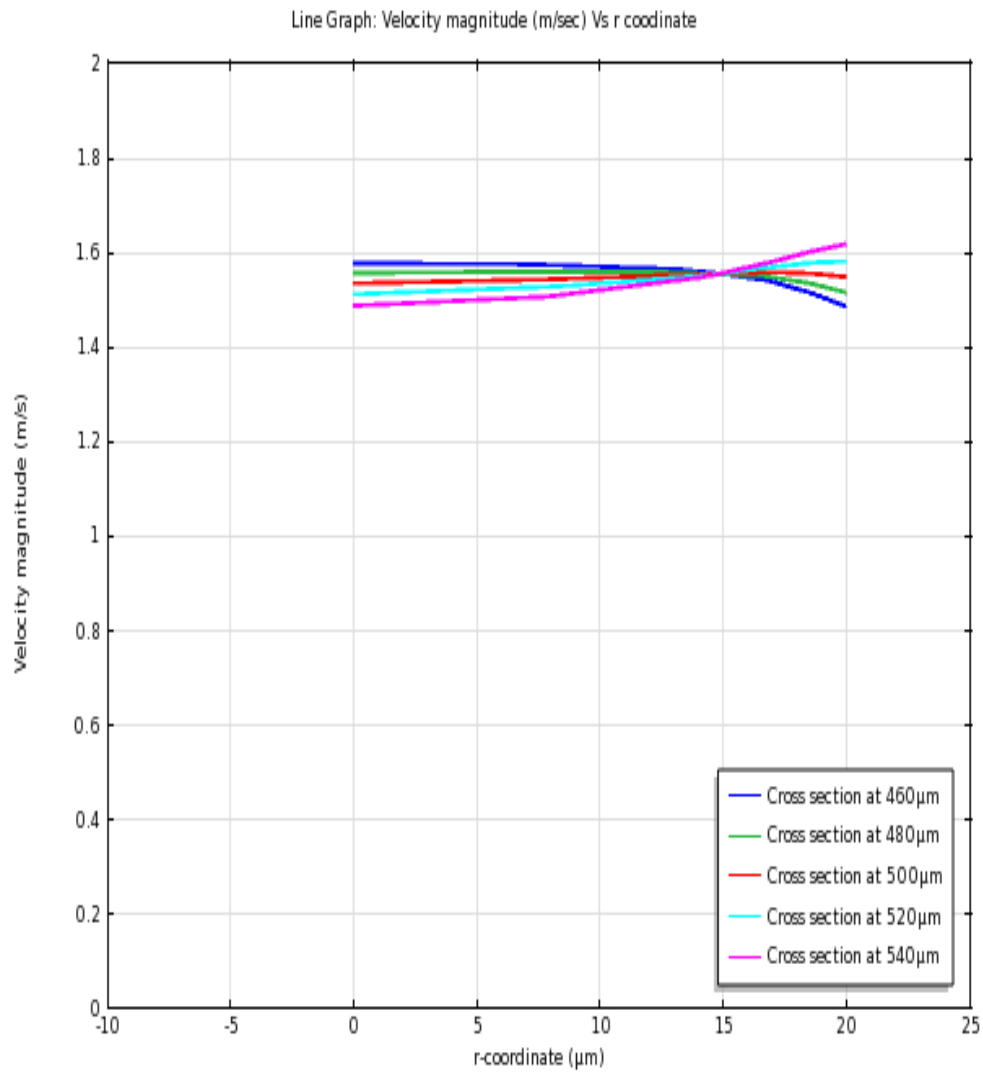


Figure : Velocity profile in a cylindrical microchannel cross section with and without Joule heating

Conclusion

- The velocity profile was significantly changed due to the presence of Joule heating and the plug like velocity profile disappeared.

References

- Baoming Li, Daniel Y. Kwok, 2003, A lattice Boltzmann model for electrokinetic microchannel flow of electrolyte solution in the presence of external forces with the Poisson–Boltzmann equation, *International Journal of Heat and Mass Transfer*, 46: 4235–4244.
- Sriram Sridharan, Joule heating effects on electrokinetic transport in constriction microchannels, M-Tech Thesis, Clemson University, May 2011
- Yuejun Kang, Chun Yang , Xiaoyang Huang, 2004, Analysis of the electroosmotic flow in a microchannel packed with homogeneous microspheres under electrokinetic wall effect, *International Journal of Engineering Science*, 42: 2011–2027.
- Z Shaoa, C.L Renb, and G.E. Schneiderc, 2009, A complete numerical model for electrokinetic flow and species transport in microchannels, *Physics Journal. Special Topics*, 171:189–194.

THANK YOU